

THIS EXAM IS CLOSED TO BOOKS AND NOTES. NO CALCULATORS ARE ALLOWED!  
Use the back of the **previous** page if more space is needed!

MA303

EXAMINATION II (Practice)

Name \_\_\_\_\_ ID # \_\_\_\_\_ Section # \_\_\_\_\_

There are 11 Problems on this booklet. For All problems, mark the answers clearly.

**Points awarded**

1. (5 pts) \_\_\_\_\_

2. (5 pts) \_\_\_\_\_

3. (5 pts) \_\_\_\_\_

4. (5 pts) \_\_\_\_\_

5. (5 pts) \_\_\_\_\_

6. (5 pts) \_\_\_\_\_

7. (5 pts) \_\_\_\_\_

8. (5 pts) \_\_\_\_\_

9. (5 pts) \_\_\_\_\_

10. (5 pts) \_\_\_\_\_

**Total Points:** \_\_\_\_\_

1. (5 points)

$$f(t) = 1 + u_2(t)(t - 2) + u_4(t)(2 - t) + u_6(t)t^2$$

The values of  $f(3)$ ,  $f(5)$  and  $f(7)$  are

- a) 10, 26, 50.
- b) 1, -3, 49.
- c) 2, 1, 49.
- d) 2, -3, 50.
- e) 2, 1, 50.

2. (5 points) Let  $s$  be a constant. Compute

$$\int_2^4 5e^{-st} dt$$

- a)  $-5(e^{-4s} - e^{-2s})$
- b)  $-\frac{5}{s}(e^{-4s} - e^{-2s})$
- c)  $5(e^{-4t} - e^{-2t})$
- d)  $\frac{5}{s}(e^{-4s} - e^{-2s})$
- e)  $10s$

3. (5 points) Compute

$$\int_0^t (t - \tau)\tau \, d\tau =$$

- a) 0
- b)  $\frac{1}{2}t^2$
- c)  $\frac{1}{6}t^3$
- d)  $-\frac{1}{2}\tau^3$
- e)  $\frac{1}{2}(t - \tau)^3$

4. (5 points)

$$f(t) = \int_0^t (t - \tau)^3 \cos(3\tau) \, d\tau$$

Find the Laplace transform of  $f(t)$ .

- a)  $\frac{6s}{s^4(s^2 + 9)}$
- b)  $\frac{18s}{s^4(s^2 + 9)}$
- c)  $\frac{6}{s^4} + \frac{3s}{s^2 + 9}$
- d)  $\frac{6}{s^4(s^2 + 9)}$
- e)  $\frac{s}{s^4(s^2 + 9)}$

5. (5 points) What is the solution of initial value problem

$$y'' = \delta(t - \pi) - \delta(t - 2\pi); \quad y(0) = y'(0) = 0.$$

- a)  $y(t) = u_\pi(t)t - u_{2\pi} + \pi$
- b)  $y(t) = \frac{1}{t^2}(e^{-\pi t} - e^{-2\pi t})$
- c)  $y(t) = c_1 + c_2 t$
- d)  $y(t) = u_\pi(t)(t - \pi) - u_{2\pi}(t)(t - 2\pi)$
- e)  $y(t) = u_\pi(t)t - u_{2\pi}t$

6. (5 points) The inverse Laplace transform of

$$F(s) = \frac{se^{-2s}}{s^2 + 4s + 13}$$

is

- a)  $u_2(t)(e^{-2t} \cos(3(t-2)) - e^{-2t} \sin(3(t-2)))$
- b)  $u_2(t)(e^{-2(t-2)} \cos(3(t-2)) - \frac{2}{3}e^{-2(t-2)} \sin(3(t-2)))$
- c)  $u_2(t)(e^{-2t} \cos(3t) - \frac{2}{3}e^{-2t} \sin(3t))$
- d)  $u_2(t)(e^{-2(t+2)} \cos(3(t+2)) - \frac{2}{3}e^{-2(t+2)} \sin(3(t+2)))$
- e)  $e^{-2(t+2)} \cos(3(t+2)) - \frac{2}{3}e^{-2(t+2)} \sin(3(t+2))$

7. (5 points)

$$f(t) = \begin{cases} t, & 0 \leq t < 4 \\ t^2 + t, & 4 \leq t < \infty. \end{cases}$$

Find the Laplace transform of  $f(t)$ .

a)  $F(s) = \frac{2}{s^3}$

b)  $F(s) = \frac{1}{s^2} + e^{-4s} \left( \frac{2}{s^3} - \frac{1}{s^2} \right)$

c)  $F(s) = \frac{1}{s^2} + e^{-4s} \left( \frac{1}{s} - \frac{1}{s^2} \right)$

d)  $F(s) = \frac{1}{s^2} + e^{-4s} \left( \frac{2}{s^3} + \frac{8}{s^2} + \frac{16}{s} \right)$

e)  $F(s) = \frac{1}{s^2} + e^{-4s} \left( \frac{2}{s^3} - \frac{8}{s^2} + \frac{16}{s} \right)$

8. (5 points) Find the Laplace transform of

$$f(t) = t \cos(2t)$$

a)  $F(s) = \frac{4 - s^2}{(s^2 + 4)^2}$

b)  $F(s) = e^{-s} \frac{s}{s^2 + 4}$

c)  $F(s) = \frac{s - 1}{(s - 1)^2 + 4}$

d)  $F(s) = \frac{1}{s(s^2 + 4)}$

e)  $F(s) = \frac{s^2 - 4}{(s^2 + 4)^2}$

9. (5 points) Solve the initial value problem

$$y'' + y = f(t); \quad y(0) = 0, \quad y'(0) = 1$$

where

$$f(t) = \begin{cases} 0 & t < 2 \\ 3 & 2 \leq t \end{cases}$$

- a)  $y(t) = \sin(t) + 3(t - 2)u_2(t) - 3u_2(t) \cos(t - 2)$
- b)  $y(t) = c_1 \cos(t) + c_2 \sin(t)$
- c)  $y(t) = \sin(t) + 3u_2(t) + 3u_2(t) \sin(t)$
- d)  $y(t) = \sin(t) + 3u_2(t) + 3u_2(t) \sin(t - 2)$
- e)  $y(t) = \sin(t) + 3u_2(t) - 3u_2(t) \cos(t - 2)$

10. (5 points) What is the solution of initial value problem

$$y'' + 2y' + 2y = \delta(t - \pi); \quad y(0) = 1, \quad y'(0) = 0.$$

- a)  $y(t) = e^{-t} \cos(t) + e^{-t} \sin(t) + u_\pi(t)e^{\pi-t} \sin(t - \pi)$
- b)  $y(t) = e^{-t} \cos(t) + 2e^{-t} \sin(t) + u_\pi(t)e^{\pi-t} \sin(t - \pi)$
- c)  $y(t) = u_\pi(t)e^{t-\pi} \sin(t - \pi)$
- d)  $y(t) = e^{-t} \cos(t) + 2e^{-t} \sin(t) + u_\pi(t)e^{\pi-t} \sin(t - \pi) + u_\pi(t)e^{\pi-t} \cos(t - \pi)$
- e)  $y(t) = e^{-t} \cos(t) + e^{-t} \sin(t) + u_\pi(t)e^{\pi-t} \cos(t - \pi)$

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EXAMINATION II (Practice) (Answer)

1. E
2. B
3. C
4. A
5. D
6. B
7. D
8. E
9. E
10. A