

Remember that your work is graded on the quality of your writing and explanation as well as the validity of the mathematics.

- (1) (10 Points) Diagonalize the following matrix, if possible.

$$\begin{bmatrix} 5 & -2 \\ 0 & 5 \end{bmatrix}$$

If not, explain why.

- (2) (10 Points) Diagonalize the following matrix, if possible.

$$A = \begin{bmatrix} 0 & -4 & -6 \\ -1 & 0 & -3 \\ 1 & 2 & 5 \end{bmatrix}$$

That is, find an invertible matrix  $P$  and a diagonal matrix  $D$  such that  $A = PDP^{-1}$ .

[Hint: the characteristic equation of given matrix can be factored:  $\det(A - \lambda I) = -(\lambda - 1)(\lambda - 2)^2$ ]