

- (1) rank = 3
- (2) (a) $a = 3$; (b) 18
- (3)
- (4) (i) and (ii)
- (5) C
- (6) C
- (7) D
- (8) E
- (9) B
- (10) None of the given answers, but $(-1 + i, 2)$.

Solution for # 10:

$$A - (-2 + i)I = \begin{bmatrix} -3 + 2 - i & -1 \\ 2 & -1 + 2 - i \end{bmatrix} = \begin{bmatrix} -1 - i & -1 \\ 2 & 1 - i \end{bmatrix}.$$

Multiply the first row by $-1 + i$ to obtain

$$\begin{bmatrix} 2 & 1 - i \\ 2 & 1 - i \end{bmatrix},$$

which reduces to

$$\begin{bmatrix} 2 & 1 - i \\ 0 & 0 \end{bmatrix}.$$

Therefore, a solution $\mathbf{v} = (v_1, v_2)$ to $(A - (-2 + i)I)\mathbf{v} = \mathbf{0}$ satisfies $2v_1 + (1 - i)v_2 = 0$. The vector $(-1 + i, 2)$ is such a solution.