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An inverse problem problem arising from magnetohydrodynamics

Given the semilinear equation $\Delta u = f(u)$ in Ω , where Ω is a two-dimensional bounded domain, with u=0 on $\partial\Omega$, we consider the problem of determining the nonlinear term $f\geq 0$ from knowledge of the normal derivative of $u,\frac{\partial u}{\partial n},$ on $\partial\Omega$. It is easy to see that the identification of f fails if Ω is a ball. We review some uniqueness results for analytic f's in classes of non-smooth domains Ω and we describe a result of uniqueness in a class of smooth domains Ω obtained recently with M. Vogelius and S. Vessella via a regularity result for the (free) boundary $\partial\Omega$.