

8 Monday, September 11

Theorem (Product Rule).

$$\frac{d}{dx} [fg] = \frac{df}{dx} g + \frac{dg}{dx} f$$

Theorem (Quotient Rule).

$$\frac{d}{dx} \left[\frac{f}{g} \right] = \frac{g \frac{df}{dx} - f \frac{dg}{dx}}{g^2}$$

Theorem (Derivatives of Trigonometric Functions).

$$(1) \quad \frac{d}{dx} [\tan x] = \sec^2 x$$

$$(2) \quad \frac{d}{dx} [\sec x] = \sec x \tan x$$

$$(3) \quad \frac{d}{dx} [\cot x] = -\csc^2 x$$

$$(4) \quad \frac{d}{dx} [\csc x] = -\csc x \cot x$$

Example. Find the derivative.

$$(1) \quad y = (3 - x^2)(x^3 - x + 1)$$

$$(2) \quad y = (x^2 + 1) \left(x + 5 + \frac{1}{x} \right)$$

$$(3) \quad y = \csc x - 6\sqrt{x} + 7$$

$$(4) \quad y = x^2 \cot x - \frac{1}{x^2}$$

$$(5) \quad y = (\sec x + \tan x) \tan x$$

$$(6) \quad y = (\sin x + \cos x) \sec x$$

$$(7) \quad y = x^2 \sin x + 2x \cos x - 2 \sin x$$

$$(8) \quad y = xe^x - e^x$$

$$(9) \quad y = (x^2 - 2x + 2) e^x$$

$$(10) \quad y = e^x \sin x + e^x \cos x$$

$$(11) \quad y = x \sin x \cos x$$

$$(12) \quad y = x^3 e^x \cos x$$

Example. Find the equation for the tangent line at the following points.

(1) $y = (x - 1)(x^2 + x + 1)$ at $c = 0$.

(2) $y = \left(x + \frac{1}{x}\right) \left(x - \frac{1}{x} + 1\right)$ at $c = 1$.

(3) $y = (9x^2 - 6x + 2)e^x$ at $c = 0$.

(4) $y = (1 + \sec x) \sin x$ at $c = \pi/4$.

(5) $y = 2e^x \tan x$ at $c = 0$.