

Review for Exam 1

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MA 158

Definition of a function

You should be able to...

- Determine when you are given a function (vertical line test)
- Given a function f , be able to find $f(\text{anything})$ and simplify
- Solve for $f(x) = 0$ or $f(x) = a$, where a is a number other than 0.

Domain and Range

You should be able to...

- Know when to use $(, [,),]$. (Brackets when point is included, parentheses when not)
- Know how to write an interval using the interval notation
- Given a graph, state the domain and range of the function
- Given a function like a polynomial, rational or square root function, state its domain

Applications of functions

You should be able to...

- Determine the domain and range in the context of a word problem
- Convert a word problem into equations and then interpret the results in the context of the problem
- Set up a system of equations relating something like Surface Area and Volume, or Perimeter and Area

Simplifying Algebraic Expressions

You should be able to...

- Given a complex fraction, simplify to a regular fraction
- Rationalize roots (multiplying by conjugate)
- Factor polynomial and rational expressions

Operations on Functions/Compositions of Functions

You should be able to...

- Add, subtract, multiply and divide functions
- Find composition of functions given a table, graph or explicit equations
- Find domain of a composition of functions

Applications of Compositions

You should be able to...

- Interpret a word problem and recognize when you are composing functions
- Determine domain in the context of a word problem

The Difference Quotient

You should be able to...

- Given any function, find the average rate of change on an interval $[a, b]$.
- Find and simplify the difference quotient of the form $\frac{f(x+h)-f(x)}{h}$ or $\frac{f(x)-f(a)}{x-a}$

Piecewise Functions

You should be able to...

- Graph a piecewise function
- Determine the domain and range of a piecewise function
- Determine y values of given x values of a piecewise function
- Interpret a piecewise-defined graph
- Apply these principles to word problems