

## Notes

## Examples

**Example 1.** Find the general solution for the differential equation

$$\frac{dy}{dx} = 14 \frac{x^7 + 3}{y^2}.$$

**Example 2.** Americium-241 is a ubiquitous isotope of Am, and is probably found in your household smoke detector. The half-life of  $^{241}\text{Am}$  is 432.2 years. If your smoke detector has 4 micrograms of  $^{241}\text{Am}$  when you move into your house, how much will remain when you pay off your 30-year mortgage?

**Example 3.** Find a particular solution to the given differential equation.

$$\frac{dy}{dx} = 6x^2 e^{5y-x^3}$$

**Example 4.** You arrive at a crime scene at 6:00 am and discover a body. Crime scene investigators measure the body's temperature to be  $27^{\circ}\text{C}$  upon arrival, and an hour later the body's temperature is  $25^{\circ}\text{C}$ . During this time, the temperature of the room was  $22^{\circ}\text{C}$ . Assuming that the person a temperature of  $37^{\circ}\text{C}$  when living, what was the time of death?

**Example 5.** Find a particular solution to the differential equation ( $n$  is a constant)

$$y' = 6x^n, \quad y(1) = 3.$$