

Please show **all** your work! Answers without supporting work will not be given credit.
Write answers in spaces provided.

Solutions

Name: _____

1. Find the derivative of $S(t) = 4t^3 \tan(t) - \sqrt{t}$

$$S(t) = \underbrace{4t^3 \tan(t)}_{\text{Product Rule}} - t^{1/2}$$

$$S'(t) = 12t^2 \tan(t) + 4t^3 \sec^2(t) - \frac{1}{2}t^{-1/2}$$

$$\frac{dS}{dt} = \frac{12t^2 \tan(t) + 4t^3 \sec^2(t)}{-\frac{1}{2}t^{-1/2}}$$

2. Given the velocity and initial position of a body moving along a coordinate line at time t , find the body's position, $s(t)$, at time t .

$$v(t) = -4t + 2, \quad s(0) = 3$$

$$\begin{aligned} s(t) &= \int v(t) dt \\ &= \int (-4t + 2) dt \\ &= -\frac{4t^2}{2} + 2t + C \\ &= -2t^2 + 2t + C \end{aligned}$$

$$\begin{aligned} \text{When } s(0) &= 3 \\ 3 &= 0 + 0 + C \\ C &= 3 \end{aligned}$$

$$s(t) = -2t^2 + 2t + 3$$

3. Evaluate the definite integral

$$\int_0^{\pi/6} (3 \cos(x) - 6) dx$$

$$= (3 \sin(x) - 6x) \Big|_0^{\pi/6}$$

$$= 3 \sin\left(\frac{\pi}{6}\right) - 6\left(\frac{\pi}{6}\right) - \left(3 \sin(0) - 6(0)\right)$$

$$= \frac{3}{2} - \pi$$

$$\boxed{\frac{3}{2} - \pi}$$

$$\int_0^{\pi/6} (3 \cos(x) - 6) dx = \underline{\hspace{2cm}} \boxed{\frac{3}{2} - \pi}$$

4. Evaluate the definite integral

$$\int_0^4 (3e^x + 2) dx$$

$$= (3e^x + 2x) \Big|_0^4$$

$$= 3e^4 + 2(4) - (3e^0 + 2(0))$$

$$= 3e^4 + 8 - 3$$

$$\boxed{3e^4 + 5}$$

$$\int_0^4 (3e^x + 2) dx = \underline{\hspace{2cm}} \boxed{3e^4 + 5}$$

5. A faucet is turned on at 9:00 am and water starts to flow into a tank at the rate of

$$r(t) = 6\sqrt{t}$$

where t is time in hours after 9:00 am and the rate $r(t)$ is in cubic feet per hour.

(a) How much water, in cubic feet, flows into the tank from 10:00 am to 1:00 pm?

$$\left. \begin{array}{l} 10:00 \text{ am} \Rightarrow 1 \text{ hr} \\ 1:00 \text{ pm} \Rightarrow 4 \text{ hrs} \end{array} \right\} \Rightarrow \int_1^4 6t^{1/2} dt$$
$$= 6 \left[\frac{2}{3} t^{3/2} \right]_1^4$$
$$= 4t^{3/2} \Big|_1^4$$
$$= 28$$

Answer: _____

28

(b) How many hours after 9:00 am will there be 121 cubic feet of water in the tank?

$$\text{Solve } \int_0^t 6\sqrt{t} dt = 121$$
$$4t^{3/2} = 121$$
$$t^{3/2} = \frac{121}{4}$$
$$t = \left(\frac{121}{4} \right)^{2/3}$$

Answer: _____

$\left(\frac{121}{4} \right)^{2/3}$

6. During a snowstorm, the rate, in inches per hour, at which the snow falls on a certain town is modeled by the function

$$R'(t) = -\cos(t) - 1.2t + 4$$

where t is measured in hours and $0 \leq t \leq 4$. Based on the model, what is the total amount of snow, in inches, that fell on town from $t = 0$ to $t = 4$? Round to one decimal place.

$$\begin{aligned}\int_0^4 R'(t) dt &= \int_0^4 (-\cos(t) - 1.2t + 4) dt \\ &= \left(-\sin(t) - \frac{1.2t^2}{2} + 4t \right) \Big|_0^4 \\ &= \left(-\sin(t) - 0.6t^2 + 4t \right) \Big|_0^4 \\ &\approx 7.16\end{aligned}$$

Answer: _____

7.16

7. Which derivative rule is undone by integration by substitution?

- (A) Power Rule
- (B) Quotient Rule
- (C) Product Rule
- (D) Chain Rule
- (E) Constant Rule
- (F) None of these

8. Which derivative rule is undone by integration by parts?

- (A) Power Rule
- (B) Quotient Rule
- (C) Product Rule
- (D) Chain Rule
- (E) Constant Rule
- (F) None of these

9. What would be the best substitution to make the solve the given integral?

$$\int e^{2x} \cos(e^{2x}) \sin^3(e^{2x}) dx$$

(Handwritten blue arrow points from the integral to the substitution below)

$$\int e^{2x} \cos(e^{2x}) [\sin(e^{2x})]^3 dx$$

$$u = \boxed{\sin(e^{2x})}$$

Always check du is in integral

10. What would be the best substitution to make the solve the given integral?

$$\int \sec^2(5x) e^{\tan(5x)} dx$$

$$u = \boxed{\tan(5x)}$$

Always check du is in integral

11. What would be the best substitution to make the solve the given integral?

$$\int \tan(5x) \sec(5x) e^{\sec(5x)} dx$$

$$u = \boxed{\sec(5x)}$$

Always check du is in
integral

12. What would be the best substitution to make the solve the given integral?

$$\int e^y \csc(e^y + 1) \cot(e^y + 1) dy$$

$$u = \boxed{e^y + 1}$$

Always check du is in
integral

13. Find the area under the curve $y = 14e^{7x}$ for $0 \leq x \leq 4$.

$$A = \int_0^4 14e^{7x} dx \quad \begin{array}{l} u = 7x \\ du = 7dx \end{array} \int 2e^u du$$

$$= 2e^u = 2e^{7x} \Big|_0^4$$

Area =

$$\boxed{2e^{28} - 2}$$

14. Evaluate the definite integral.

$$\int_0^2 (5e^{2x} + 8) dx$$

$$\begin{aligned} \underbrace{\int_0^2 5e^{2x} dx}_{u\text{-sub}} + \int_0^2 8 dx &= \left. \frac{5}{2} e^{2x} \right]_0^2 + \left. 8x \right]_0^2 \\ &= \frac{5}{2} (e^4 - e^0) + 8(2 - 0) \\ &= \frac{5}{2} e^4 - \frac{5}{2} + 16 \\ &= \frac{5}{2} e^4 - \frac{27}{2} \end{aligned}$$

$$\int_0^2 (5e^{2x} + 8) dx = \boxed{\frac{5}{2} e^4 + \frac{27}{2}}$$

15. Evaluate the indefinite integral.

$$\int 18x \cos(5x^2) dx$$

$$\begin{aligned} \underline{u = 5x^2} \\ \underline{du = 10x dx} \\ \frac{du}{10x} = dx \end{aligned}$$

$$\begin{aligned} \int \cancel{18x} \cos(u) \frac{du}{\cancel{10x}} &= \int \frac{9}{5} \cos(u) du \\ &= \frac{9}{5} \sin(u) + C \\ &= \frac{9}{5} \sin(5x^2) + C \end{aligned}$$

$$\int 18x \cos(5x^2) dx = \boxed{\frac{9}{5} \sin(5x^2) + C}$$

16. Evaluate the indefinite integral.

$$\int 9x^3 e^{-x^4} dx$$

$$\frac{u = -x^4}{du = -4x^3 dx}$$

$$\frac{du}{-4x^3} = dx$$

$$\int 9x^3 e^u \frac{du}{-4x^3} = -\frac{9}{4} \int e^u du$$

$$= -\frac{9}{4} e^u = -\frac{9}{4} e^{-x^4} + C$$

$$\int 9x^3 e^{-x^4} dx = \boxed{-\frac{9}{4} e^{-x^4} + C}$$

17. Evaluate the indefinite integral

$$\int x(x^2 + 4)^3 dx$$

$$\frac{u = x^2 + 4}{du = 2x dx}$$

$$\frac{du}{2x} = dx$$

$$\int \cancel{x} u^3 \frac{du}{\cancel{2x}} = \frac{1}{2} \int u^3 du = \frac{1}{2} \cdot \frac{u^4}{4} + C$$

$$= \frac{1}{8} (x^2 + 4)^4 + C$$

$$\int x(x^2 + 4)^3 dx = \boxed{\frac{1}{8} (x^2 + 4)^4 + C}$$

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18. After an oil spill, a company uses oil-eating bacteria to help clean up. It is estimated that t hours after being placed in the spill, the bacteria will eat the oil at a rate of

$$L'(t) = \sqrt{3t+2} \text{ gallons per hour.}$$

How many gallons of oil will the bacteria eat in the first 4 hours? Round to 4 decimal places.

$$\begin{aligned} \text{i.e. } \int_0^4 (3t+2)^{1/2} dt & \quad \frac{u=3t+2}{du=3dt} \quad \int u^{1/2} \frac{du}{3} \\ & \quad \frac{du}{3} = dt \\ & = \frac{1}{3} \cdot \frac{2}{3} u^{3/2} = \frac{2}{9} (3t+2)^{3/2} \Big|_0^4 \\ & \approx 11.0122 \end{aligned}$$

Answer: _____

11.0122

19. It is estimated that t -days into a semester, the average amount of sleep a college math student gets per day $S(t)$ changes at a rate of

$$\frac{-4t}{e^{t^2}} = -4te^{-t^2}$$

hours per day. When the semester begins, math students sleep an average of 8.2 hours per day. What is $S(t)$, 2 days into the semester?

$$\textcircled{1} \int -4te^{-t^2} dt \quad \begin{array}{l} u = -t^2 \\ du = -2t dt \\ \frac{du}{-2t} = dt \end{array} \quad \int \frac{-4t e^u}{-2t} du$$

$$= \int 2e^u du = 2e^u + C \\ = 2e^{-t^2} + C$$

$$\textcircled{2} S(0) = 8.2 \text{ Find } C.$$

$$8.2 = 2e^0 + C$$

$$8.2 = 2 + C$$

$$C = 6.2$$

$$\textcircled{3} S(t) = 2e^{-t^2} + 6.2$$

$$S(2) = 2e^{-4} + 6.2$$

$$\approx 6.237$$

Answer:

6.237

20. A biologist determines that, t hours after a bacterial colony was established, the population of bacteria in the colony is changing at a rate given by

$$P'(t) = \frac{5e^t}{1+e^t}$$

million bacteria per hour, $0 \leq t \leq 5$.

If the bacterial colony started with a population of 1 million, how many bacteria, in millions are present in the colony after the 5-hour experiment?

$$\begin{aligned} \textcircled{1} \int \frac{5e^t}{1+e^t} dt & \quad \begin{array}{l} u=1+e^t \\ du=e^t dt \\ \frac{du}{e^t} = dt \end{array} \quad \int \frac{\cancel{5e^t}}{u} \frac{du}{\cancel{e^t}} = \int \frac{5}{u} du \\ & = 5 \ln|u| + C \\ & = 5 \ln|1+e^t| + C \end{aligned}$$

$$\textcircled{2} P(0) = 1 \text{ Find } C.$$

$$1 = 5 \ln|1+e^0| + C$$

$$1 = 5 \ln|1+1| + C$$

$$1 = 5 \ln 2 + C$$

$$1 - 5 \ln 2 = C$$

$$\textcircled{3} P(t) = 5 \ln|1+e^t| + 1 - 5 \ln 2$$

$$P(5) = 5 \ln|1+e^5| + 1 - 5 \ln 2$$

$$\approx 22.57$$

Answer: 22.57

21. Evaluate the definite integral.

$$\int_0^{\pi/4} 3 \sin(2x) dx$$

$$\begin{aligned} \frac{u=2x}{\frac{du=2dx}{\frac{du}{2}=dx}} & \left\{ \begin{aligned} 3 \sin(u) \frac{du}{2} &= \frac{3}{2} \int \sin(u) du = -\frac{3}{2} \cos(u) \\ &= -\frac{3}{2} \cos(2x) \Big|_0^{\pi/4} \\ &= -\frac{3}{2} \cos\left(\frac{2\pi}{4}\right) - \left(-\frac{3}{2} \cos(0)\right) \end{aligned} \right. \end{aligned}$$

$$\int_0^{\pi/4} 3 \sin(2x) dx = \boxed{3/2}$$

22. Evaluate the indefinite integral.

$$\int (x+4)\sqrt{x^2+8x} dx$$

$$\begin{aligned} \frac{u=x^2+8x}{\frac{du=(2x+8)dx}{\frac{du}{2}=(x+4)dx}} & \left\{ \begin{aligned} \cancel{(x+4)} \sqrt{u} \frac{du}{2\cancel{(x+4)}} & \\ &= \frac{1}{2} \int u^{1/2} du \\ &= \frac{1}{2} \cdot \frac{2}{3} u^{3/2} + C \\ &= \frac{1}{3} (x^2+8x)^{3/2} + C \end{aligned} \right. \end{aligned}$$

$$\int (x+4)\sqrt{x^2+8x} dx = \boxed{\frac{1}{3} (x^2+8x)^{3/2} + C}$$

23. Evaluate the definite integral.

$$\int_0^9 \frac{dx}{2\sqrt{x}(\sqrt{x}+1)}$$

$$\begin{aligned} u &= \sqrt{x}+1 \\ u &= x^{1/2}+1 \\ \hline du &= \frac{1}{2}x^{-1/2} dx \end{aligned}$$

$$du = \frac{1}{2} \cdot \frac{1}{\sqrt{x}} dx$$

$$2\sqrt{x} du = dx$$

$$\begin{aligned} \int \frac{\cancel{2\sqrt{x}} du}{\cancel{2\sqrt{x}} \cdot u} &= \int \frac{du}{u} = \ln|u| \\ &= \ln|\sqrt{x}+1| \Big|_0^9 \\ &= \ln|\sqrt{9}+1| - \ln|\sqrt{0}+1| \\ &= \ln(4) \end{aligned}$$

$$\int_0^9 \frac{dx}{2\sqrt{x}(\sqrt{x}+1)} =$$

$$\boxed{\ln(4)}$$

24. Evaluate the indefinite integral.

$$\int x\sqrt{x+2} dx$$

$$\begin{aligned} \rightarrow \frac{u=x+2}{du=dx} & \int x\sqrt{u} du \\ \rightarrow \frac{x=u-2}{du=dx} & \int (u-2)u^{1/2} du \\ &= \int u^{3/2} - 2u^{1/2} du \\ &= \frac{2}{5}u^{5/2} - 2 \cdot \frac{2}{3}u^{3/2} + C \end{aligned}$$

$$\int x\sqrt{x+2} dx = \boxed{\frac{2}{5}(x+2)^{5/2} - \frac{4}{3}(x+2)^{3/2} + C}$$

25. A tree is transplanted and after t years is growing at a rate

$$r'(t) = 1 + \frac{1}{(t+1)^2} \quad \text{meters per year.}$$

After 2 years it has reached a height of 5 meters. How tall was the tree when it was originally transplanted? Round to one decimal place.

$$\begin{aligned} r(t) &= \int \left(1 + \frac{1}{(t+1)^2} \right) dt \\ &= \int (1 + (t+1)^{-2}) dt \\ &= t + \frac{(t+1)^{-1}}{-1} + C \\ &= t - \frac{1}{t+1} + C \end{aligned}$$

Find C w/ $r(2) = 5$ | So $r(t) = t - \frac{1}{t+1} + \frac{10}{3}$

$$\begin{aligned} 5 &= 2 - \frac{1}{2+1} + C \\ 3 + \frac{1}{3} &= C \\ \frac{10}{3} &= C \end{aligned}$$
$$\begin{aligned} r(0) &= 0 - 1 + \frac{10}{3} \\ &= \frac{7}{3} \approx 2.3 \end{aligned}$$

Height =

2.3

26. The marginal revenue from the sale of x units of a particular product is estimated to be $R'(x) = 50 + 350xe^{-x^2}$ dollars per unit, and where $R(x)$ is revenue in dollars. What revenue should be expected from the sale of 100 units? Assume that $R(0) = 0$.

$$\begin{aligned} R(x) &= \int 50 + 350xe^{-x^2} dx \\ &= \int 50 dx + \int 350xe^{-x^2} dx \\ &\quad \begin{aligned} u &= -x^2 \\ du &= -2x dx \\ \frac{du}{-2x} &= dx \end{aligned} \\ &= \int 50 dx + \int 350x e^u \frac{du}{-2x} \\ &= \int 50 dx - 175 \int e^u du \\ &= 50x - 175e^u + C \\ &= 50x - 175e^{-x^2} + C \end{aligned}$$

$$R(0) = 0$$

$$0 = 0 - 175 + C$$

$$C = 175$$

$$R(x) = 50x - 175e^{-x^2} + 175$$

$$R(100) \approx 5175$$

$R(100) =$ _____

5175

27. Evaluate the indefinite integral

$$\int \frac{\ln(7x)}{x} dx$$

$$\begin{aligned} u &= \ln(7x) \\ du &= \frac{1}{7x} \cdot 7 dx \\ du &= \frac{1}{x} dx \end{aligned}$$

$$\int u du = \frac{u^2}{2} = \frac{(\ln(7x))^2}{2} + C$$

$$\int \frac{\ln(7x)}{x} dx =$$

$$\frac{(\ln(7x))^2}{2} + C$$

28. Evaluate

$$\int_1^e \frac{\ln(x^4)}{x} dx$$

Rewrite $\int_1^e \frac{4 \ln x}{x} dx$ $\frac{u = \ln x}{du = \frac{1}{x} dx}$ $\int 4u du = \frac{4u^2}{2} = 2u^2 = 2(\ln x)^2 \Big|_1^e$
 $= \frac{2(\ln e)^2}{2} - \frac{2(\ln 1)^2}{2}$
 $= 2$

$$\int_1^e \frac{\ln(x^4)}{x} dx =$$

2

29. Evaluate

$$\int_e^4 \frac{dx}{x(\ln(x))^2}$$

$$\begin{aligned} u &= \ln(x) \\ du &= \frac{1}{x} dx \\ x du &= dx \end{aligned}$$

$$\int \frac{\cancel{x} du}{\cancel{x} u^2} = \int u^{-2} du = \frac{u^{-1}}{-1}$$

$$= \left. -\frac{1}{\ln x} \right]_e^4 = -\frac{1}{\ln(4)} - \left(-\frac{1}{\ln(e)} \right)$$

$$\int_e^4 \frac{dx}{x(\ln(x))^2} = \boxed{-\frac{1}{\ln(4)} + 1}$$

30. Evaluate the definite integral.

$$\int_0^{\pi/2} (x-1) \sin(x) dx$$

$$\begin{aligned} u &= x-1 \\ du &= dx \end{aligned}$$

$$\begin{aligned} dv &= \sin(x) dx \\ v &= -\cos(x) \end{aligned}$$

$$\begin{aligned} uv - \int v du &= -(x-1)\cos x \Big|_0^{\pi/2} - \int_0^{\pi/2} (-\cos x) dx \\ &= -(x-1)\cos x \Big|_0^{\pi/2} + \sin(x) \Big|_0^{\pi/2} \\ &= -\left(\frac{\pi}{2}-1\right)\cos\left(\frac{\pi}{2}\right) - [-(0-1)\cos(0)] \\ &\quad + \sin\left(\frac{\pi}{2}\right) - \sin(0) \\ &= -1 + 1 = 0 \end{aligned}$$

$$\int_0^{\pi/2} (x-1) \sin(x) dx = \boxed{0}$$

31. Evaluate

$$\int 3x \ln(x^7) dx$$

Rewrite $\int 3x(7 \ln(x)) dx = \int 21x \ln x dx$

$$\begin{aligned} \frac{u=21 \ln(x)}{du=\frac{21}{x} dx} \quad \frac{dv=x dx}{v=\frac{x^2}{2}} \quad uv - \int v du \\ = \frac{21x^2 \ln x}{2} - \int \frac{x^2}{2} \cdot \frac{21}{x} dx \\ = \frac{21x^2 \ln x}{2} - \int \frac{21}{2} x dx \\ = \frac{21x^2 \ln x}{2} - \frac{21 \cdot x^2}{2} + C \\ = \frac{21x^2 \ln x}{2} - \frac{21x^2}{4} + C \end{aligned}$$
$$\int 3x \ln(x^7) dx = \frac{21x^2 \ln x}{2} - \frac{21x^2}{4} + C$$

32. Evaluate

$$\int x^3 \ln(2x) dx$$

$$\begin{aligned} \frac{u=\ln(2x)}{du=\frac{1}{2x} \cdot 2 dx} \quad \frac{dv=x^3 dx}{v=\frac{x^4}{4}} \quad uv - \int v du = \frac{x^4 \ln(2x)}{4} - \int \frac{x^4}{4} \cdot \frac{1}{x} dx \\ = \frac{x^4 \ln(2x)}{4} - \frac{1}{4} \int x^3 dx \\ = \frac{x^4 \ln(2x)}{4} - \frac{1}{4} \cdot \frac{x^4}{4} + C \end{aligned}$$

$$\int x^3 \ln(2x) dx = \frac{x^4 \ln(2x)}{4} - \frac{x^4}{16} + C$$

33. Evaluate the indefinite integral

$$\int \sqrt{x} \ln(x) dx$$

$$\frac{u = \ln(x) \quad dv = x^{1/2} dx}{du = \frac{1}{x} dx \quad v = \frac{2}{3} x^{3/2}} \quad uv - \int v du$$

$$du = \frac{1}{x} dx \quad v = \frac{2}{3} x^{3/2}$$

$$= \frac{2}{3} x^{3/2} \ln(x) - \int \frac{2}{3} x^{3/2} \cdot \frac{1}{x} dx$$

$$= \frac{2}{3} x^{3/2} \ln(x) - \frac{2}{3} \int x^{1/2} dx$$

$$= \frac{2}{3} x^{3/2} \ln(x) - \frac{2}{3} \cdot \frac{2}{3} x^{3/2} + C$$

$$\int \sqrt{x} \ln(x) dx = \frac{\frac{2}{3} x^{3/2} \ln(x)}{-\frac{4}{9} x^{3/2} + C}$$

34. Evaluate the definite integral.

$$\int_0^3 x e^{3x} dx$$

$$\frac{u = x \quad dv = e^{3x} dx}{du = dx \quad v = \frac{1}{3} e^{3x}} \quad uv - \int v du$$

$$= \frac{x}{3} e^{3x} - \int \frac{1}{3} e^{3x} dx$$

$$= \left(\frac{x}{3} e^{3x} - \frac{1}{3} \cdot \frac{e^{3x}}{3} \right) \Big|_0^3$$

$$= \frac{3}{3} e^9 - \frac{1}{9} e^9 - \left[0 - \frac{1}{9} \right]$$

$$= \frac{2}{9} e^9 + \frac{1}{9}$$

$$\int_0^3 x e^{3x} dx = \frac{8}{9} e^9 + \frac{1}{9}$$

35. The population of pink elephants in Dumbo's dreams, in hundreds, t years after the year 1980 is given by

$$P(t) = \frac{e^{5t}}{1 + e^{5t}}$$

What is the average population during the decade between 1980 and 2000?

$$\text{i.e. } \frac{1}{2000-1980} \int_0^{20} \frac{e^{5t}}{1+e^{5t}} dt \quad \begin{array}{l} u=1+e^{5t} \\ du=5e^{5t}dt \\ \frac{du}{5e^{5t}}=dt \end{array} \quad \frac{1}{20} \int \frac{e^{5t}}{u} \cdot \frac{du}{5e^{5t}}$$

$$= \frac{1}{100} \int \frac{du}{u} = \frac{1}{100} \ln|u|$$

$$= \frac{1}{100} \ln|1+e^{5t}| \Big|_0^{20}$$

$$\approx 0.9931$$

0.9931 hundreds or 993

Answer:

36. Evaluate the indefinite integral.

$$\int 20x \sin(2x) dx$$

$$\begin{array}{l} u=20x \quad dv=\sin(2x)dx \\ du=20dx \quad v=-\frac{\cos(2x)}{2} \end{array} \quad uv - \int v du$$

$$= -\frac{20}{2}x \cos(2x) + \int \frac{20}{2} (+\cos(2x)) dx$$

$$= -10x \cos(2x) + 10 \int \cos(2x) dx$$

$$= -10x \cos(2x) + 10 \frac{\sin(2x)}{2} + C$$

$$-10x \cos(2x) + 5 \sin(2x) + C$$

$$\int 20x \sin(2x) dx = \underline{\hspace{10em}}$$

37. The velocity of a cyclist during an hour-long race is given by the function

$$v(t) = 166te^{-2.2t} \text{ mi/hr}, \quad 0 \leq t \leq 1$$

Assuming the cyclist starts from rest, what is the distance in miles he traveled during the first hour of the race?

$$\begin{aligned} \textcircled{1} \int 166te^{-2.2t} dt \\ \frac{u=166t}{du=166dt} \quad \frac{dv=e^{-2.2t} dt}{v=\frac{e^{-2.2t}}{-2.2}} \quad uv - \int v du \\ = \frac{166t e^{-2.2t}}{-2.2} + \int \frac{e^{-2.2t}}{+2.2} \cdot 166 dt \\ = -\frac{166t e^{-2.2t}}{2.2} + \frac{166}{2.2} \cdot \frac{e^{-2.2t}}{-2.2} + C \\ = -\frac{166t e^{-2.2t}}{2.2} - \frac{166 e^{-2.2t}}{(2.2)^2} + C \end{aligned}$$

$$\textcircled{2} s(0) = 0. \text{ Find } C.$$

$$0 = 0 - \frac{166}{(2.2)^2} + C \rightarrow C = \frac{166}{(2.2)^2}$$

$$\textcircled{3} s(t) = -\frac{166t e^{-2.2t}}{2.2} - \frac{166 e^{-2.2t}}{(2.2)^2} + \frac{166}{(2.2)^2}$$

$$s(1) = -\frac{166}{2.2} e^{-2.2} - \frac{166}{(2.2)^2} e^{-2.2} + \frac{166}{(2.2)^2}$$

$$\approx 22.137$$

$$\boxed{22.137}$$

Answer: _____

38. After t days, the growth of a plant is measured by the function $2000te^{-20t}$ inches per day. What is the change in the height of the plant (in inches) after the first 14 days?

$$\int_0^{14} 2000te^{-20t} dt$$

$$\begin{aligned} u &= 2000t & dv &= e^{-20t} dt & uv &- \int v du \\ du &= 2000 dt & v &= \frac{e^{-20t}}{-20} \end{aligned}$$

$$= 2000t \left(\frac{e^{-20t}}{-20} \right) + \int \left(\frac{e^{-20t}}{+20} \right) 2000 dt$$

$$= -100te^{-20t} + 100 \int e^{-20t} dt$$

$$= -100te^{-20t} + 100 \left(\frac{e^{-20t}}{-20} \right)$$

$$= \left(-100te^{-20t} - 5e^{-20t} \right) \Big|_0^{14}$$

$$= 5$$

Answer:

5