

$$\bullet (a \pm b)^2 = a^2 \pm 2ab + b^2$$

$$\bullet x^{-m} = \frac{1}{x^m}$$

$$\bullet a^2 - b^2 = (a+b)(a-b)$$

$$\bullet \sqrt[q]{x^p} = x^{p/q}$$

Trick to multiply terms

$$h(x) = (2x+1)(3x^2+2x+1) = 6x^3 + 7x^2 + 4x + 1$$

	$3x^2$	$2x$	1
$2x$	$6x^3$	$4x^2$	$2x$
1	$3x^2$	$2x$	1

$$\tan x = \frac{\sin x}{\cos x}$$

$$\csc x = \frac{1}{\sin x}$$

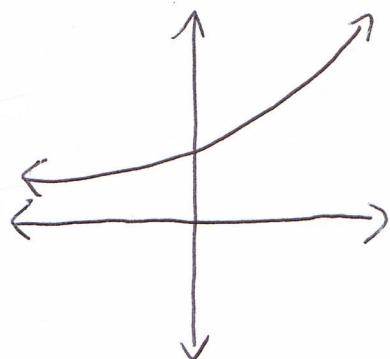
$$\cot x = \frac{\cos x}{\sin x}$$

$$\sec x = \frac{1}{\cos x}$$

Remember

$$e^x > 0$$

Never! $e^x \neq 0$



Vertical Asymptote vs. Hole

Hole when factors cancel out. $f(x) = \frac{x^2(x-4)}{x-4}$

If no cancellation, then VA. $f(x) = \frac{1}{x}$

Remember $\sin^2 x = [\sin x]^2 \neq \sin(x^2)$

Logarithmic Properties

a) $\ln e^x = x$

b) $\ln(ab) = \ln(a) + \ln(b)$

c) $\ln\left(\frac{a}{b}\right) = \ln(a) - \ln(b)$

d) $\ln(a^x) = x \ln(a)$

Quadratic Formula

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

'a-c' method for factoring

Ex. $4x^2 - 4x - 3$

First find $ac = 4 \cdot (-3) = -12$

Next list all factors of $ac = -12$

$$\begin{array}{l} \text{ } \\ \begin{array}{c|cc} & 1 & 12 \\ & 2 & 6 \\ & 3 & 4 \end{array} \end{array}$$

yield $b = -4$

The idea is to add the factors to yield $b = -4$

Note since $ac = -12$ and $b = -4$ the largest factor

gets a negative. So

$$ac = -12$$

$$\begin{array}{r} \wedge \\ 1 - 12 = -11 \\ 2 - 6 = -4 = b \\ 3 - 4 = -1 \end{array}$$

Rewrite the middle term with the numbers in the pink box.

$$4x^2 - 4x - 3 = 4x^2 + \boxed{2}x - 6x - 3$$

Now factor by grouping.

$$= 2x(2x+1) - 3(2x+1)$$

Check that the parenthesis match.

$$= (2x-3)(2x+1)$$