

MA 16010 LESSON 34: NUMERICAL INTEGRATION (Examples w/ Solutions)

EX 1: Use the Trapezoid Rule to approximate $\int_0^3 x^2 dx$ using $n = 3$. Round your answer to the nearest tenth.

Solution: (1) First calculate Δx .

$$\begin{aligned}
 a &= \underline{0} \\
 b &= \underline{3} \\
 b - a &= \underline{3 - 0 = 3} \\
 \Delta x &= \frac{b - a}{n} = \underline{\frac{3}{3} = 1}
 \end{aligned}$$

(2) Determine what $f(x)$ is.

$$\int_0^3 \boxed{x^2} dx$$

Hence $f(x) = \underline{x^2}$

(3) Find the following values:

$x_0 = \underline{0}$	$f(x_0) = \underline{0}$
$x_1 = \underline{1}$	$f(x_1) = \underline{1}$
$x_2 = \underline{2}$	$f(x_2) = \underline{4}$
$x_3 = \underline{3}$	$f(x_3) = \underline{9}$

$f(x_0) = \underline{0}$
$2 \cdot f(x_1) = \underline{2}$
$2 \cdot f(x_2) = \underline{8}$
$f(x_3) = \underline{9}$

(4) Sum all the values in the black box. = 19

(5) Multiply the value found in (4), Δx found in (1), and $1/2$, which yields our answer.

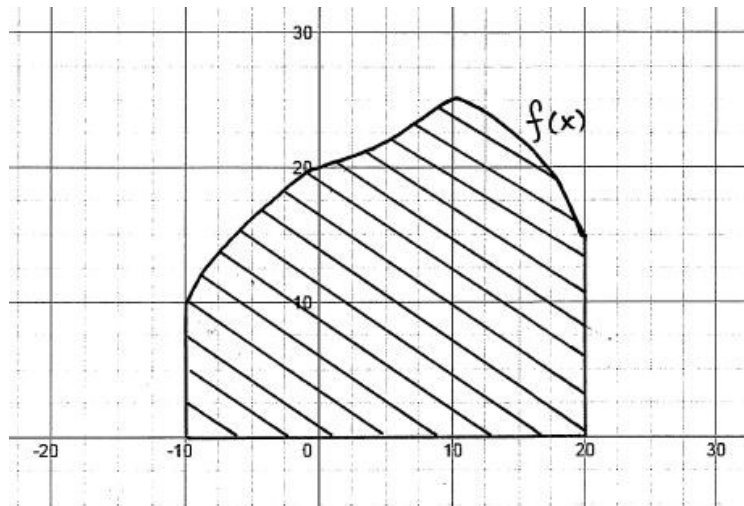
$$\underline{19 \times 1 \times \frac{1}{2} = \frac{19}{2}}$$

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EX 2: Approximate the area of the shaded region by using the Trapezoid Rule with $n = 3$

Solution: (1) First calculate Δx .

$$\begin{aligned}
 a &= \underline{-10} \\
 b &= \underline{20} \\
 b - a &= \underline{20 - (-10) = 30} \\
 \Delta x &= \frac{b - a}{n} = \underline{\frac{30}{3} = 10}
 \end{aligned}$$



(2) Find the following values:

$$\begin{array}{ll}
 x_0 = \underline{-10} & f(x_0) = \underline{10} \\
 x_1 = \underline{0} & f(x_1) = \underline{20} \\
 x_2 = \underline{10} & f(x_2) = \underline{25} \\
 x_3 = \underline{20} & f(x_3) = \underline{15}
 \end{array}$$

$$\begin{array}{ll}
 f(x_0) &= \underline{10} \\
 2 \cdot f(x_1) &= \underline{40} \\
 2 \cdot f(x_2) &= \underline{50} \\
 f(x_3) &= \underline{15}
 \end{array}$$

(3) Sum all the values in the black box. = 115

(4) Multiply the value found in (3), Δx found in (1), and $1/2$, which yields our answer.

$$\underline{115 \times 10 \times \frac{1}{2} = 575}$$