

Please show **all** your work! Answers without supporting work will not be given credit.
Write answers in spaces provided.

Name: _____

1. [5 pts] Write the Left and Right Riemann Sums with 20 rectangles to estimate the area under the curve $\sin(2x + 4) - 14$ on the interval of $[60, 80]$.

Solution:

$$\Delta x = \frac{80 - 60}{20} = \frac{20}{20} = 1 \quad [1 \text{ pt}]$$

$$x_i = a + i \cdot \Delta x = 60 + i \quad [1 \text{ pt}]$$

$$f(x_i) = \sin(2(60 + i) + 4) - 14 = \sin(124 + 2i) - 14 \quad [1 \text{ pt}]$$

Using the above, we find

$$L_n = \sum_{i=0}^{n-1} f(x_i) \cdot \Delta x \Rightarrow L_{20} = \sum_{i=0}^{19} \sin(124 + 2i) - 14 \quad [1 \text{ pt}]$$

$$R_n = \sum_{i=1}^n f(x_i) \cdot \Delta x \Rightarrow R_{20} = \sum_{i=1}^{20} \sin(124 + 2i) - 14 \quad [1 \text{ pt}]$$

2. [5 pts] Write the Left and Right Riemann Sums with 10 rectangles to estimate the area under the curve $3 \ln(x^2)$ on the interval of $[0, 50]$.

Solution:

$$\Delta x = \frac{50 - 0}{10} = \frac{50}{10} = 5 \quad [1 \text{ pt}]$$

$$x_i = a + i \cdot \Delta x = 5i \quad [1 \text{ pt}]$$

$$f(x_i) = 3 \ln(5i)^2 = 3 \ln(25i^2) \quad [1 \text{ pt}]$$

Using the above, we find

$$L_n = \sum_{i=0}^{n-1} f(x_i) \cdot \Delta x \Rightarrow L_{10} = \sum_{i=0}^9 3 \ln(25i^2) \quad [1 \text{ pt}]$$

$$R_n = \sum_{i=1}^n f(x_i) \cdot \Delta x \Rightarrow R_{10} = \sum_{i=1}^{10} 3 \ln(25i^2) \quad [1 \text{ pt}]$$