

MA 16020 Exam 2 Study Guide : Cal 1

Important Limits to know for the exam

$$y = e^{-ax}$$

$$\lim_{x \rightarrow -\infty} [e^{-ax}] = +\infty$$

$$\lim_{x \rightarrow \infty} [e^{-ax}] = 0$$

$$y = e^{ax}$$

$$\lim_{x \rightarrow -\infty} [e^{ax}] = 0$$

$$\lim_{x \rightarrow \infty} [e^{ax}] = \infty$$

$$y = \ln(ax)$$

$$\lim_{x \rightarrow 0^+} [\ln(ax)] = -\infty$$

$$\lim_{x \rightarrow \infty} [\ln(ax)] = \infty$$

$$y = \frac{1}{x}$$

$$\lim_{x \rightarrow \infty} \left[\frac{1}{x} \right] = 0$$

$$\lim_{x \rightarrow -\infty} \left[\frac{1}{x} \right] = 0$$

$$y = \frac{1}{x^2}$$

$$\lim_{x \rightarrow -\infty} \left[\frac{1}{x^2} \right] = 0$$

$$\lim_{x \rightarrow \infty} \left[\frac{1}{x^2} \right] = 0$$

Also polynomials as $x \rightarrow \infty$, the limit goes to $\pm \infty$

Differentiation Rules

Integration Rules

$$\frac{d}{dx}(c) = 0$$

$$\int 0 dx = c$$

$$\frac{d}{dx}(nx) = k$$

$$\int k dx = kx + C$$

$$\frac{d}{dx}(nf(x)) = kf'(x)$$

$$\int kf'(x) dx = kf(x) + C$$

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C \text{ when } n \neq -1$$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\int \cos x dx = \sin x + C$$

$$\frac{d}{dx}(\cos x) = -\sin x$$

$$\int \sin x dx = -\cos x + C$$

$$\frac{d}{dx}(\tan x) = \sec^2 x$$

$$\int \sec^2 x dx = \tan x + C$$

$$\frac{d}{dx}(\cot x) = -\csc^2 x$$

$$\int \csc^2 x dx = -\cot x + C$$

$$\frac{d}{dx}(\sec x) = \sec x \tan x$$

$$\int \sec x \tan x dx = \sec x + C$$

$$\frac{d}{dx}(\csc x) = -\csc x \cot x$$

$$\int \csc x \cot x dx = -\csc x + C$$

$$\frac{d}{dx}(e^x) = e^x$$

$$\int e^x dx = e^x + C$$

$$\frac{d}{dx}(\ln x) = \frac{1}{x}, x > 0$$

$$\int \frac{1}{x} dx = \ln|x| + C$$

• Note if the integral has bounds we do not use $+C$.

• Always take derivative of your answer, before evaluating when integrating. Especially when you have trig functions!!!