

$$\bullet (a \pm b)^2 = a^2 \pm 2ab + b^2$$

$$\bullet x^{-m} = \frac{1}{x^m}$$

$$\bullet a^2 - b^2 = (a+b)(a-b)$$

$$\bullet \sqrt[q]{x^p} = x^{p/q}$$

Trick to multiply terms

$$h(x) = (2x+1)(3x^2+2x+1) = 6x^3 + 7x^2 + 4x + 1$$

| | | | |
|------|--------|--------|------|
| | $3x^2$ | $2x$ | 1 |
| $2x$ | $6x^3$ | $4x^2$ | $2x$ |
| 1 | $3x^2$ | $2x$ | 1 |

$$\tan x = \frac{\sin x}{\cos x}$$

$$\csc x = \frac{1}{\sin x}$$

$$\cot x = \frac{\cos x}{\sin x}$$

$$\sec x = \frac{1}{\cos x}$$

| | 0 | $\pi/6$ | $\pi/4$ | $\pi/3$ | $\pi/2$ |
|-----|-----------------------|-----------------------|-----------------------|-----------------------|---------------------------|
| sin | $0/\cancel{2}$ | $1/\cancel{2}$ | $\sqrt{2}/\cancel{2}$ | $\sqrt{3}/\cancel{2}$ | $\sqrt{4}/\cancel{2} = 1$ |
| cos | $\sqrt{4}/\cancel{2}$ | $\sqrt{3}/\cancel{2}$ | $\sqrt{2}/\cancel{2}$ | $1/\cancel{2}$ | $0/\cancel{2} = 0$ |

Remember $\sin^2 x = [\sin x]^2 \neq \sin(x^2)$

Logarithmic Properties

① $\ln e^x = x$

② $\ln(ab) = \ln(a) + \ln(b)$

③ $\ln\left(\frac{a}{b}\right) = \ln(a) - \ln(b)$

④ $\ln(a^x) = x \ln(a)$

a-c method for factoring

Ex. $4x^2 - 4x - 3$

First find $ac = 4 \cdot (-3) = -12$

Next list all factors of $ac = -12$

$$\begin{array}{l} 1 \ 12 \\ 2 \ 6 \\ 3 \ 4 \end{array}$$

The idea is to add the factors to yield $b = -4$
Note since $ac = -12$ and $b = -4$ the largest factor

gets a negative. So

$$ac = -12$$

$$\begin{array}{r} 1 - 12 = -11 \\ 2 - 6 = -4 = b \\ 3 - 4 = -1 \end{array}$$

Rewrite the middle term with the numbers in the pink box.

$$4x^2 - 4x - 3 = 4x^2 + \boxed{2}x - 6x - 3$$

Now factor by grouping.

$$= 2x(2x+1) - 3(2x+1)$$

Check that the parenthesis match.

$$= (2x-3)(2x+1)$$