

Proposition 41: If a triangle shares a side with a parallelogram, and the third vertex of the triangle lies on the extended opposite side of the parallelogram, then the area of the parallelogram is twice that of the triangle.

Proof: Let ABC and $ABDE$ be a triangle and a parallelogram with C on DE . We need to show $\text{Area}(ABDE) = 2\text{Area}(\triangle ABC)$. By postulate 1, we draw BE . Since $EC \parallel AB$, $\text{Area}(\triangle ABE) = \text{Area}(\triangle ABC)$, by Proposition 37. By Proposition 34, $\text{Area}(ABDE) = 2\text{Area}(\triangle ABE)$. Thus, by CN1, $\text{Area}(ABDE) = 2\text{Area}(\triangle ABC)$, as claimed. QED

