Test 1 Fall 2019

October 1, 2019

1. (6 points) You are given that $_tq_{90}=\frac{t^2}{100}$ for $0 \le t \le 10$.

Calculate e_{90} .

2. (8 points) The curtate expectation of life, which is $\it e_{80}$, is 10.606 based on the Standard Ultimate Life Table.

If $\,q_{80}=0.015\,$ instead of 0.032658, but the other mortality rates are unchanged, determine $\,e_{80}\,$ accurate to three decimal places.

3. (10 points) You are given the following mortality table:

x	q_x
90	0.2
91	0.4

You are also given that deaths are uniformly distributed between ages 90 and 91 and the deaths follow a constant force of mortality between ages 91 and 92.

Calculate $_{0.2\mid 0.9}q_{90.2}$.

4. (10 points) Let Z be the present value random variable for a discrete whole life policy with a death benefit of 100 sold to (101) who has just been underwritten.

You are given the following select and ultimate mortality table:

[x]	$q_{[x]}$	$q_{\scriptscriptstyle [x]+1}$	q_{x+2}	x+2
100	0.05	0.15	0.35	102
101	0.10	0.30	0.50	103
102	0.20	0.40	0.80	104
103	0.25	0.50	1.00	105

You are also given that d=0.07 .

Calculate $\mathit{Var}[Z]$.

5. (9 points) You are given:

i.
$$A_{60} = 0.500$$

ii.
$$^2A_{60} = 0.350$$

iii.
$$p_{60} = 0.96$$

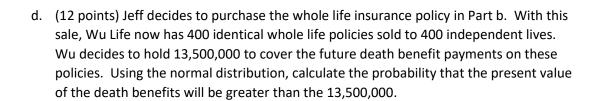
iv.
$$p_{61} = 0.95$$

v.
$$i = 0.06$$

Let Z be the present value random variable for a whole life to (61) with a death benefit of 1 paid at the end of the year of death.

Calculate the Var(Z).

6.	Jeff is (63). He wants to buy a life insurance policy from Wu Life Insurance Company. However, he is not sure which policy to buy. All calculations assume:
	i. Mortality follows the Standard Ultimate Life Table
	ii. $i = 0.05$
	iii. Deaths are uniformly distributed between integral ages.
	First, he decides to consider a whole life insurance policy that pays a death benefit of 100,000 at the end of the year of death. Jeff asks Shina who is the chief actuary at Wu Life to do several things for him.
	a. (4 points) Write the present value random variable Z for this policy.
	 b. (4 points) Jeff estimates that the expected present value of this whole life policy is 33,000 to the nearest 1000. Calculate it to the nearest 1.
	 c. (4 points) What would be the expected present value of the whole life policy if it paid a death benefit at the moment of death instead of at the end of the year of death.



e. (8 points) Jeff asks Shina to calculate his median future life time. The median future life time is the point at which $_{n+s}$ $p_{63}=0.5$ where $0 \le s \le 1$. Jeff knows that n=25 .

Determine s accurate to three decimal places.

f.	(10 points) Jeff decides to also purchase a term insurance policy that pays a death benefit of 100,000 payable at the moment of death if he dies in the next 26 years. Determine the expected present value of this term insurance.
g.	(5 points) Explain why the expected present value of the term insurance is less than the expected present value of the whole life insurance.

7. (10 points) Alisa (20) buys a special whole life policy with a non-level death benefit. The death benefits are paid at the end of the year of death and are listed in the following table:

Years	Death Benefit
1-30	125,000
31-50	300,000
51+	50,000

Using the Standard Ultimate Life Table with $\,i=5\%$, calculate the expected present value of this insurance.

STAT 472

Test 1

Fall 2019

October 1, 2019

1. (6 points) You are given that
$$_tq_{90}=\frac{t^2}{100}$$
 for $0 \le t \le 10$.

Calculate $\mu_{\!\scriptscriptstyle 95}$.

2. (9 points) Under the Standard Ultimate Life Table:

a.
$$e_{60:\overline{10}} = 9.733$$

b.
$$e_{70:\overline{10}} = 9.201$$

c.
$$e_{80} = 10.606$$

Determine $e_{{
m 60}}$.

3. (12 points) You are given the following mortality table:

Х	q_x
90	0.2
91	0.4
92	0.6
93	0.8
94	1.0

Let Z be the present value random variable for a discrete three year term insurance policy issued to (90) with a death benefit of 5,000 paid at the end of the year of death.

You are also given that d = 0.10.

Calculate Var[Z] .

4. (10 points) You are given the following select and ultimate mortality table:

[x]	$q_{[x]}$	$q_{\scriptscriptstyle [x]+1}$	q_{x+2}	x+2
100	0.05	0.15	0.025	102
101	0.10	0.30	0.50	103
102	0.20	0.40	0.80	104
103	0.25	0.50	1.00	105

During the first two years, deaths are assumed to be distributed uniformly between integral ages. After two years, it is assumed that we have a constant force of mortality between integral ages.

Calculate $_{0.7\mid 0.9}q_{[101]+0.6}$.

5. (10 points) There are currently 1000 independent lives all age 80 who own life insurance policies at Maxwell Life Insurance Company.

You are given that mortality for these policies follows Gompertz Law with $B\!=\!0.000005$ and $c\!=\!1.10$.

Let L_{90} be the random variable representing the number of lives alive at the end of 10 years.

Calculate the $Var(L_{90})$.

6.	Jeff is (70). He wants to buy a life insurance policy from Lai Life Insurance Company. Howev	er,
	he is not sure which policy to buy. All calculations assume:	

- i. Mortality follows the Standard Ultimate Life Table
- ii. i = 0.05
- iii. Deaths are uniformly distributed between integral ages.

First, he decides to consider a whole life insurance policy that pays a death benefit of 100,000 at the moment of death. Jeff asks Jake who is the chief actuary at Lai Life to do several things for him.

a. (4 points) Write the present value random variable Z for this policy.

b. (5 points) Jeff estimates that the expected present value of this whole life policy is 44,000 to the nearest 1000. Calculate it to the nearest 1.

c.	(10 points) Calculate the probability that Z is less than 51,000. The probability needs to be accurate to 3 decimal places.

d.	(10 points) Jeff decides to purchase a 13 year endowment insurance policy with a death benefit of 100,000 payable at the end of the year of death.
	Determine the expected present value of this endowment insurance.
e.	(5 Points) Explain why the expected present value of the endowment insurance is
	greater than the expected present value of the whole life insurance.

7. (10 points) Jimmy (30) buys a special 45 year term insurance policy with a non-level death benefit. The death benefits are paid at the end of the year of death and are listed in the following table:

Years	Death Benefit
1-20	100,000
21-35	50,000
36-45	25,000

Using the Standard Ultimate Life Table with $\,i=5\%$, calculate the expected present value of this insurance.

8. (9 points) You are given:

i. Z is the present value for a whole life policy sold to (x) with a death benefit of 1 payable at the end of the year of death.

ii.
$$^{2}A_{x}=0.41$$

iii.
$$Var(Z) = 0.05$$

iv.
$$q_x = 0.035$$

v.
$$q_{x+1} = 0.037$$

vi.
$$i = 0.06$$

Calculate $A_{\mathbf{x}+\mathbf{2}}$ accurate to 4 decimal places.