

### Homework 8

Due Wednesday, November 17th at the beginning of class. Justify your answers. Please let me know if you have a question or find a mistake.

1. Exercise 19.3.2 from page 263. Use the Riemann sum theorem (Theorem 19.3) the fundamental theorem of calculus (Theorem 20.1), and the fact that  $\frac{d}{dx} \ln(1 + x^2) = 2x/(1 + x^2)$ .
2. Parts (a) and (b) of Exercise 19.4.2 from page 264.

*Hint:* For part (a), show using the definition of continuity that, given such an  $f$ , there are an interval  $I$  contained in  $[a, b]$  and a constant  $d > 0$  such that the function  $h$  defined by

$$h(x) = \begin{cases} d, & x \text{ in } I, \\ 0, & \text{otherwise,} \end{cases}$$

obeys  $h(x) \leq f(x)$  for all  $x$  in  $[a, b]$ .

3. Exercise 19.4.3 from page 264. Use the result of part (b) of Exercise 19.4.2 and an inequality for  $\sin x$  from Chapter 15.
4. Exercise 20.2.1 from page 282.