

### Homework 6

Due October 21st on paper at the beginning of class. Please let me know if you have a question or find a mistake.

1. Exercise 18 from page 100.
2. Exercise 1 from page 114.
3. Exercise 3 from page 114.
4. Exercise 6 from page 114.

*Hint:* Use the mean value theorem on  $[0, x]$  to show that  $f(x) \leq xf'(x)$ .

5. Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be differentiable and suppose  $f(x) = f(x + 1)$  for all  $x$ . Prove that  $f'$  has infinitely many zeroes.