## Linquan Ma

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RESEARCH	$\label{lem:commutative} \begin{tabular}{ll} Commutative Algebra and Algebraic Geometry: singularities, multiplicities, local cohomology, and the homological conjectures. \end{tabular}$		
Education	University of Michigan, Ann Arbor, Michigan, USA  Ph.D., Mathematics Advisor: Melvin Hochster Thesis: The Frobenius endomorphism and multiplicities		
	Peking University, Beijing, China B.S., Mathematics Advisor: Jiazhong Yang		2004-2008
Employment	Associate Professor, Purdue University 2021		2021-
	Assistant Professor, Purdue University		2018-2021
	Research Assistant Professor, University of Utah		2015–2018
	Golomb Visiting Assistant Professor, Purdue University 2014		2014-2015
VISITING POSITIONS	von Neumann Fellow, IAS 2025–2026		
	Research Member, SLMath/MSRI Spring 2024		
	Research Member, IAS Fall 2023		
	Research Member, MSRI	$A_{\mathrm{I}}$	pr–May 2019
Honors & Grants	<ul> <li>University Faculty Scholar, Pur</li> <li>Alfred P. Sloan Research Fellow</li> <li>NSF FRG Grant DMS-1952366 Algebraic geometry and singula (with Bhargav Bhatt, Christoph Karl Schwede, Karen Smith and</li> <li>NSF Grant DMS-1901672: Sing</li> <li>Don Tucker Outstanding Postdo</li> </ul>	rship  5: Collaborative Research: rities in positive and mixed characteristic her Hacon, Sándor Kovács, Mircea Mustaţă, d Chenyang Xu) gularities and multiplicities in commutative algebra	2023–2028 2023 2020–2024 2020–2024 2019–2023 2017 2016–2019 2015–2016
	<ul><li>AMS-Simons Travel Grant</li><li>President Fellowship, Peking United States</li></ul>	niversity	2015–2016 2006–2007

# Papers & Preprints

- 48 F-singularities: a commutative algebra approach (with Thomas Polstra), last updated 2025.
- 47 An introduction to singularities in commutative algebra via perfectoid big Cohen-Macaulay algebras (with Kevin Tucker), *Contemp. Math.*, to appear. (A short proof of the direct summand theorem via the flatness lemma, unpublished note).
- 46 Lim Cohen-Macaulay sequences of modules (with Bhargav Bhatt and Melvin Hochster).
- 45 Perfectoid pure singularities (with Bhargav Bhatt, Zsolt Patakfalvi, Karl Schwede, Kevin Tucker, Joe Waldron and Jakub Witaszek).
- 44 Non-existence of Ulrich modules over Cohen-Macaulay local rings (with Srikanth Iyengar, Mark Walker and Ziquan Zhuang).
- 43 Test ideals in mixed characteristic: a unified theory up to perturbation (with Bhargav Bhatt, Zsolt Patakfalvi, Karl Schwede, Kevin Tucker, Joe Waldron and Jakub Witaszek).
- 42 Colength, multiplicity, and ideal closure operations II (with Pham Hung Quy and Ilya Smirnov), *Michigan Math. J.*, to appear.
- 41 Perfectoid signature, perfectoid Hilbert-Kunz multiplicity, and an application to local fundamental groups (with Hanlin Cai, Seungsu Lee, Karl Schwede and Kevin Tucker). (Perfectoid signature and applications, Oberwolfach Report 6/2023, 338-339.)
- 40 Vanishing and non-negativity of the first normal Hilbert coefficient (with Pham Hung Quy), *Acta Math. Vietnam.* 49 (2024), no. 3, 311-325 (special issue dedicated to Ngo Viet Trung).
- 39 Regularity, singularities and h-vector of graded algebras (with Hailong Dao and Matteo Varbaro), Trans. Amer. Math. Soc. 377 (2024), no. 3, 2149-2167.
- 38 Lim Ulrich sequences and Boij-Söderberg cones (with Srikanth Iyengar and Mark Walker), Forum Math. Sigma 11 (2023), Paper No. e115, 26 pp.
- 37 Uniform Lech's inequality (with Ilya Smirnov), Proc. Amer. Math. Soc. 151 (2023), no. 6, 2387-2397.
- 36 Globally +-regular varieties and the minimal model program for threefolds in mixed characteristic (with Bhargav Bhatt, Zsolt Patakfalvi, Karl Schwede, Kevin Tucker, Joe Waldron and Jakub Witaszek), Publ. Math. Inst. Hautes Études Sci. 138 (2023), 69-227.
- 35 Lim Ulrich sequences and Lech's conjecture, Invent. Math. 231 (2023), no. 1, 407-429.
- 34 Symbolic power containments in singular rings in positive characteristic (with Eloísa Grifo and Karl Schwede), *Manuscripta Math.* 170 (2023), no. 3-4, 471-496.
- 33 A Buchsbaum theory for tight closure (with Pham Hung Quy), Trans. Amer. Math. Soc. 375 (2022), no. 11, 8257-8276.
- 32 Multiplicities and Betti numbers in local algebra via lim Ulrich points (with Srikanth Iyengar and Mark Walker), *Algebra Number Theory* 16 (2022), no. 5, 1213-1257.
- 31 F-stable secondary representations and deformation of F-injectivity (with Alessandro De Stefani), *Acta Math. Vietnam.* 47 (2022), no. 1, 141-150 (special issue dedicated to Nguyen Tu Cuong).
- 30 An analog of adjoint ideals and PLT singularities in mixed characteristic (with Karl Schwede, Kevin Tucker, Joe Waldron and Jakub Witaszek), *J. Algebraic Geom.* 31 (2022), no. 3, 497-559.
- 29 Maximal Cohen-Macaulay complexes and their uses: a partial survey (with Srikanth Iyengar, Karl Schwede and Mark Walker), *Commutative Algebra*, 475-500, Springer, Cham, 2021 (dedicated to David Eisenbud).
- 28 Koszul and local cohomology, and a question of Dutta (with Anurag Singh and Uli Walther), *Math. Z.* 298 (2021), no. 1-2, 697-711.
- 27 Covers of rational double points in mixed characteristic (with Javier Carvajal-Rojas, Thomas Polstra, Karl Schwede and Kevin Tucker), J. Singul. 23 (2021), 127-150.
- 26 Singularities in mixed characteristic via perfectoid big Cohen-Macaulay algebras (with Karl Schwede), *Duke Math. J.* 170 (2021), no. 13, 2815-2890.

- 25 Cohomologically full rings (with Hailong Dao and Alessandro De Stefani), Int. Math. Res. Not. IMRN 2021, no. 17, 13508-13545.
- 24 Extended plus closure in complete local rings (with Raymond Heitmann), *J. Algebra* 571 (2021), 134-150 (special issue dedicated to Craig Huneke).
- 23 Asymptotic Lech's inequality (with Craig Huneke, Pham Hung Quy and Ilya Smirnov), Adv. Math. 372 (2020), 107296, 33 pp.
- 22 Filter regular sequence under small perturbations (with Pham Hung Quy and Ilya Smirnov), *Math. Ann.* 378 (2020), no. 1-2, 243-254.
- 21 Colength, multiplicity, and ideal closure operations (with Pham Hung Quy and Ilya Smirnov), Comm. Algebra 48 (2020), no. 4, 1601-1607.
- 20 A Kunz-type characterization of regular rings via alterations (with Karl Schwede), J. Pure Appl. Algebra 224 (2020), no. 3, 1124-1131.
- 19 Recent applications of p-adic methods to commutative algebra (with Karl Schwede), Notices Amer. Math. Soc. 66 (2019), no. 6, 820-831.
- 18 F-signature under birational morphisms (with Thomas Polstra, Karl Schwede and Kevin Tucker), Forum Math. Sigma, 7 (2019), e11, 20 pp.
- 17 Lech's inequality, the Stückrad-Vogel conjecture, and uniform behavior of Koszul homology (with Patricia Klein, Pham Hung Quy, Ilya Smirnov and Yongwei Yao), Adv. Math. 347 (2019), 442-472. (Lech's inequality and the Stückrad-Vogel conjecture, Oberwolfach Report 6/2019, 428-429.)
- 16 Regular rings and perfect(oid) algebras (with Bhargav Bhatt and Srikanth Iyengar), Comm. Algebra 47 (2019), no. 6, 2367-2383 (special issue dedicated to Gennady Lyubeznik).
- 15 Maximal Cohen-Macaulay modules over certain Segre products, *Comm. Algebra* 47 (2019), no. 6, 2488-2493 (special issue dedicated to Gennady Lyubeznik).
- 14 Perfectoid multiplier/test ideals in regular rings and bounds on symbolic powers (with Karl Schwede), *Invent. Math.* 214 (2018), no. 2, 913-955.
- 13 Big Cohen-Macaulay algebras and the vanishing conjecture for maps of Tor in mixed characteristic (with Raymond Heitmann), *Algebra Number Theory* 12 (2018), no. 7, 1659-1674.
- 12 D-module and F-module length of local cohomology modules (with Mordechai Katzman, Ilya Smirnov and Wenliang Zhang), Trans. Amer. Math. Soc. 370 (2018), no. 12, 8551-8580.
- 11 F-singularities under generic linkage (with Janet Page, Rebecca R.G., William Taylor and Wenliang Zhang), J. Algebra 505 (2018), 194-210.
- 10 Frobenius actions on local cohomology modules and deformation (with Pham Hung Quy), Nagoya Math. J. 232 (2018), 55-75.
- 9 The dualizing complex of F-injective and Du Bois singularities (with Bhargav Bhatt and Karl Schwede), Math. Z. 288 (2018), no. 3-4, 1143-1155.
- 8 The vanishing conjecture for maps of Tor and derived splinters, J. Eur. Math. Soc. (JEMS), 20 (2018), no. 2, 315-338.
- 7 Lech's conjecture in dimension three, Adv. Math. 322 (2017), 940-970. (Lech's conjecture, Oberwolfach Report 57/2016, 3214-3216.)
- 6 Local cohomology of Du Bois singularities and applications to families (with Karl Schwede and Kazuma Shimomoto), *Compos. Math.* 153 (2017), no. 10, 2147-2170.
- 5 F-injectivity and Buchsbaum singularities, Math. Ann. 362 (2015), no. 1-2, 25-42.
- 4 Eulerian graded D-modules (with Wenliang Zhang), Math. Res. Lett. 21 (2014), no. 1, 149-167.
- 3 A sufficient condition for F-purity, J. Pure Appl. Algebra 218 (2014), 1179-1183.
- 2 The category of F-modules has finite global dimension, J. Algebra 402 (2014), 1-20.
- 1 Finiteness properties of local cohomology for F-pure local rings, Int. Math. Res. Not. IMRN 2014, no. 20, 5489-5509.

# INVITED SPEAKER LECTURE SERIES

- Conference on Algebraic Geometry, Tianyuan Mathematical Research Center (TMRC) in Kunming, Sep 2025.
- RGAS Summer School on Perfectoid Techniques, La Cristalera, Autonomous University of Madrid, May 2025.
- Introductory Workshop: Commutative Algebra, SLMath/MSRI, Berkeley, Jan 2024.
- Special month in Ann Arbor on Algebraic Geometry, University of Michigan, May 2023.
- MAGNTS: Midwest Arithmetic Geometry and Number Theory Series, UIC, Oct 2022.
- Graduate Course on Tight Closure of Ideals and its Applications, ICTP Virtual Meeting, May–Jun 2022 (online).
- MSRI graduate school, Thematic Program in Commutative Algebra and its Interaction with Algebraic Geometry, Center for Mathematics at Notre Dame, Jun 2019.
- Frobenius Action in Commutative Algebra: Recent Developments, Institute of Mathematics of the University of Barcelona, Jan 2019.
- RTG mini-course: Topics in Commutative Algebra, University of Utah, May 2018.
- Homological Conjectures in Commutative Algebra, UIC, Nov 2016.

## CONFERENCE, WORKSHOP & COLLOQUIUM TALKS

- Singularities in algebra and geometry: a conference honoring the mathematical contributions of Karen E. Smith, CIMAT, Jun 2025.
- P-adic and Characteristic p Methods in Algebraic Geometry, Bernoulli Center, Lausanne, Jun 2025.
- Commutative Algebra in mixed characteristic, University of Nebraska, Mar 2025.
- Singularities and Symmetries at Texas, Texas A&M University, Feb 2025.
- Fall school on Methods in Mixed Characteristic Geometry, Johannes Gutenberg University of Mainz, Oct 2024 (online).
- Commutative Algebra and Singularity Theory (in Honor of the 80th Birthday of Professor Keiichi Watanabe), Osaka Metropolitan University, Sep 2024.
- Conference on Commutative Algebra and its Interaction with Algebraic Geometry and Algebraic Combinatorics (A Conference on the occasion of Uwe Nagel's 60th Birthday), University of Notre Dame, Aug 2024.
- Colloquium in a summer school in Algebra and Number Theory, Academy of Mathematics and Systems Science (AMSS), Chinese Academy of Sciences, Jul 2024.
- Conference on p-adic Geometry and Related Topics, Beijing International Center for Mathematical Research (BICMR), Peking University, Jun 2024.
- University of Alabama Colloquium, Mar 2024.
- Algebra and Number Theory Forum, Sichuan University, Dec 2023 (online).
- Special Session in Commutative Algebra for the 56th Congress of the Mexican Mathematical Society, Oct 2023 (online).
- p-adic Hodge theory mini workshop, Princeton University, Oct 2023.
- AMS Special session on Commutative algebra, differential operators, and singularities, Creighton University, Oct 2023.
- Georgia State University Colloquium, Oct 2023.
- Morgantown Algebra Days, West Virginia University, Apr 2023.
- AMS Special session on Homological methods in commutative algebra, University of Cincinnati, Apr 2023.
- Yau Mathematical Sciences Center (YMSC) Colloquium, Apr 2023 (online).

- Resolutions in Local Algebra and Singularity Theory, Oberwolfach Workshop, Feb 2023.
- Written Geometry: Commutative Algebra, CIRM, Luminy, Jan 2023.
- Clay Mathematics Institute workshop p-adic Hodge Theory and Applications, Mathematical Institute of the University of Oxford, Sep 2022.
- AMS Special Session on Commutative Ring Theory, University of New Mexico, Albuquerque, Oct 2021 (online).
- Singularities in Positive Characteristic, CIRM, Luminy, Jul 2021 (online).
- Early Commutative Algebra Researchers, Jun 2020 (online).
- JMM Special Session on Commutative Algebra, Denver, Jan 2020.
- KUMUNU-regional commutative algebra conference, University of Nebraska, Sep 2019.
- Conference on Commutative Algebra and its Interaction with Algebraic Geometry (In Honor of Bernd Ulrich), Center for Mathematics at Notre Dame, Jun 2019.
- New Mexico State University Colloquium, Mar 2019.
- Singularities and Homological Aspects of Commutative Algebra, Oberwolfach Workshop, Feb 2019.
- The 40th Japan Symposium on Commutative Algebra, LecTore Hayama, Kanagawa, Nov 2018.
- Modern Algebraic Geometry, Beijing International Center for Mathematical Research (BICMR), Peking University, Jul 2018.
- AMS Special Session on Commutative Algebra, Vanderbilt University, Nashville, Apr 2018.
- University of Minnesota Colloquium, Apr 2018.
- Mini-workshop on Commutative Algebra, University of Virginia, Mar 2018.
- The Homological Conjectures: Resolved! MSRI, Berkeley, Mar 2018.
- AMS Special Session on Homological Methods in Commutative Algebra, University of North Texas, Sep 2017.
- Local Cohomology in Commutative Algebra and Algebraic Geometry (on occasion of Gennady Lyubeznik's 60th birthday), University of Minnesota, Aug 2017.
- AMS Special Session on Commutative Algebra, Indiana University, Bloomington, Apr 2017.
- Young Mathematician Forum, Beijing International Center for Mathematical Research (BICMR), Peking University, Dec 2016.
- Asymptotic Phenomena in Local Algebra and Singularity Theory, Oberwolfach Workshop, Dec 2016.
- Purdue University Special Colloquium, Nov 2016.
- Higher Dimensional Algebraic Geometry and Characteristic p, CIRM, Luminy, Sep 2016.
- Midwest Commutative Algebra Conference, Purdue University, Aug 2015.
- Recent developments in positive characteristic techniques in commutative algebra: Frobenius Operators and Cartier Algebras, Atlanta, Mar 2015.
- AMS Special Session on Commutative Algebra, Albuquerque, Apr 2014.
- JMM Special Session on Homological and Characteristic p Methods in Commutative Algebra, Baltimore, Jan 2014.
- Birational Geometry and Singularities in Positive Characteristic, University of Tokyo, Nov 2013.

#### SEMINAR TALKS

- Fellowship of the Ring, A worldwide commutative algebra seminar, Mar 2024, Apr 2020 (online).
- UCSB Geometry and Arithmetic Seminar, Feb 2024.
- Johns Hopkins Algebraic Geometry Seminar, Dec 2023.

- Princeton Algebraic Geometry Seminar, Nov 2023, Feb 2018, Apr 2017.
- IAS Special Year Seminar, Oct 2023.
- UIC Algebraic Geometry Seminar and Commutative Algebra Seminar, Sep 2023, Mar 2021 (online), Oct 2016, Oct 2013.
- Purdue University Commutative Algebra Seminar and Algebraic Geometry Seminar, Feb 2022 (online), Sep 2021, Jan 2020, Feb 2019, Nov 2018, Sep 2018, Oct 2015, Apr 2015, Jan 2015, Dec 2014, Nov 2014, Oct 2014.
- Zoom Algebraic Geometry Seminar, Dec 2021 (online).
- Northwestern Algebraic Geometry Seminar, Oct 2021 (online).
- Purdue Bridge to Research Seminar, Oct 2021.
- CUNY Commutative Algebra & Algebraic Geometry Seminar, Apr 2021 (online).
- IIT Bombay Virtual Commutative Algebra seminar, Aug 2020 (online).
- Joint NU/UIC/UofC algebraic geometry and commutative algebra seminar, May 2020 (online).
- BICMR/Peking University Algebraic Geometry Seminar, Dec 2019.
- University of Utah Commutative Algebra Seminar and Algebraic Geometry Seminar, Nov 2019, Mar 2019, Nov 2018, Sep 2017, Nov 2015, Nov 2015, Oct 2014.
- University of Michigan Commutative Algebra Seminar, Dec 2018, Nov 2015, Nov 2014, Feb 2014, Oct 2013, Oct 2012, Jan 2012, Dec 2011.
- University of Kentucky Algebra Seminar, Oct 2018.
- University of Minnesota Algebra Seminar, Apr 2018.
- University of Tokyo Algebraic Geometry Seminar, Dec 2017.
- UCSD Algebraic Geometry Seminar, Apr 2017.
- University of Kansas Algebra Seminar, Oct 2016.
- University of Virginia Algebra Seminar, May 2016.
- University of Arkansas Algebra Seminar, Oct 2015.
- UIUC Commutative Ring Theory Seminar, Feb 2015.
- University of Notre Dame Algebraic Geometry/Commutative Algebra Seminar, Dec 2014.
- University of Nebraska Commutative Algebra Seminar, Jan 2014.
- MSRI/UC Berkeley Commutative Algebra Seminar, May 2013.
- Penn State University Algebra and Number Theory Seminar, Feb 2013.

#### Organization

- Co-organizer, Singularities, *D*-modules, and Connections to Physics, BIRS program at Banff, Sep 2025.
- Co-organizer, Birational geometry in positive and mixed characteristics and connections to commutative algebra (one of the afternoon sessions of 2025 Summer Research Institute in algebraic geometry), Colorado State University, Jul 2025.
- Co-organizer, Algebra Across Time: a conference in honor of Bill Heinzer, Purdue University, Apr 2025.
- Co-organizer, RayFest: a celebration of the mathematics of Raymond Heitmann, University of Nebraska, Apr 2025.
- Co-organizer, Recent Developments in Commutative Algebra, SLMath/MSRI, Apr 2024.
- Co-organizer, Algebraic Geometry and Singularities Learning Workshop & Conference, University of Washington, Seattle, Jun 2022.
- Co-organizer, Advances in Mixed Characteristic Commutative Algebra and Geometric Connections, BIRS program at Casa Matematica Oaxaca (CMO) Mexico, May 2022 (hybrid conference).

- Co-organizer, AMS Special Session on Recent Developments in Commutative Algebra, West Lafayette, Mar 2022 (online).
- Co-organizer, *D*-modules, Group Actions, and Frobenius: Computing on Singularities, Topical Workshop at ICERM, Providence, Aug 2021 (online).
- Co-organizer, AMS Special Session on Advances in Commutative Algebra, Ann Arbor, Oct 2018.
- Assistant, Commutative Algebra and Related Topics, MSRI Summer School, Okinawa Institute of Science and Technology, May 2017.
- Co-organizer, AMS Special Session on Commutative Algebra, Salt Lake City, Apr 2016.
- Co-organizer, JMM Special Session on Commutative Algebra, Seattle, Jan 2016.
- Assistant, MRC Commutative Algebra Program, Snowbird, Utah, Jun 2015.
- Local organizer, Computational workshop on Frobenius singularities and invariants, University of Michigan, May 2012.

### Professional Service

- Editor: Bulletin and Journal of the London Mathematical Society, 2023–
- Editor: Nagoya Mathematical Journal, 2023– (Associate Editor during 2022–2023)
- Referee for: Advances in Mathematics, Algebra and Number Theory, Annales Scientifiques de l'École Normale Supérieure\*, Annali della Scuola Normale Superiore di Pisa Classe di Scienze, Annals of Mathematics\*, Canadian Journal of Mathematics\*, Colloquium Mathematicum\*, Communications in Algebra, Compositio Mathematica, Duke Mathematical Journal, Épijournal de Géométrie Algébrique\*, Forum of Mathematics Pi\*, International Mathematics Research Notices, Inventiones mathematicae\*, Journal für die reine und angewandte Mathematik\*, Journal of Algebra, Journal of Algebra, Journal of Pure and Applied Algebra, Journal of the American Mathematical Society, Journal of the European Mathematical Society, Journal of the Institute of Mathematics of Jussieu, Manuscripta Mathematica, Mathematical Proceedings of the Cambridge Philosophical Society\*, Mathematische Annalen\*, Mathematical Proceedings of the American Mathematical Society\*, Michigan Mathematical Journal, Nagoya Mathematical Journal\*, Pacific Journal of Mathematics, Proceedings of the American Mathematical Society, Publications Mathématiques Institut de Hautes Études Scientifiques\*, Research in the Mathematical Sciences, Selecta Mathematica\*, Transactions of the American Mathematical Society. (\*=quick opionion)
- NSF Panelist, various years.
- Reviewer for AMS Mathematical Reviews and Zentralblatt Math.

### DEPARTMENTAL SERVICE

- Co-organizer, Commutative Algebra Seminar at Purdue University, 2022–2023, 2024–
- Undergraduate Majors committee, 2024-
- Undergraduate Scholarship committee, 2024-
- Graduate committee, 2022–2023.

#### MENTORING

#### Graduate students:

- Manay Batavia (co-advised with Uli Walther), 2024–
- Qiurui Li, 2020–2024.
- Cheng Meng (co-advised with Giulio Caviglia), 2021–2023.

### Postdocs:

• Farrah Yhee (co-mentored with Irena Swanson), 2021–2023.

#### Visiting students:

- Kaito Kimura (Nagoya University), Fall 2024.
- Luis Duarte (University of Genova), Feb-Mar 2022.

#### Thesis committee:

- 2025: Justin Fong
- 2024: Qiurui Li, Jiamin Li (UIC)
- 2023: Cheng Meng, Hunter Simper
- 2022: Anna-Rose Wolff, Yevgeniya Tarasova, Vinh Nguyen, Yihui Liang, Vaibhav Pandey (Utah), McKinley Gray (UIC)
- 2021: Daniel Bath
- 2020: Edward Price, Monte Cooper, Tan Dang, Roberto Ulloa Esquivel
- 2019: Alessandra Costantini, Avi Steiner
- 2018: Christina Jamroz

#### Oral exam committee:

- 2024: Manav Batavia
- 2022: Justin Fong
- 2021: Qiurui Li
- 2020: Peter McDonald (Utah), Adam LaClair
- 2019: Josiah Banks, Kyle Flanagan, Hunter Simper

## TEACHING EXPERIENCE

## Teaching at Purdue:

- Math 35100 Elementary Linear Algebra (Spring 2025, Spring 2022).
- Math 45000 Algebra Honors (Fall 2024, Fall 2021, Fall 2020, Fall 2019).
- Math 69000 Topics in Commutative Algebra: Positive characteristic methods (Fall 2024, Spring 2021).
- Math 37500 Introduction to Discrete Mathematics (Spring 2023).
- Math 69000 Topics in Commutative Algebra: Complete intersections (Fall 2022).
- Math 69000 Topics in Commutative Algebra: Homological conjectures/theorems and perfectoid spaces (Spring 2020).
- Math 26500 Linear Algebra (Fall 2018, Spring 2015, Fall 2014).

#### Teaching at Utah:

- Math 7830 Topics in Commutative Algebra: Perfectoid spaces and the homological conjectures (Spring 2018).
- Math 2210 Calculus 3 (Fall 2017, Spring 2016).
- Math 2200 Introduction to Discrete Mathematics (Spring 2017, Fall 2016).
- Math 2250 Differential Equations and Linear Algebra (Fall 2015).

#### Teaching at Michigan:

- TA for a course on Fibonacci numbers (Summer 2014).
- TA for Math 215 Calculus 3 (Spring 2014, Fall 2013, Fall 2012, Spring 2012).
- Math 116 Calculus 2 (Spring 2011).

- $\bullet$  Math 115 Calculus 1 (Spring 2010, Fall 2009).
- Math 105 Data, Functions and Graphs (Spring 2009, Fall 2008).