

Notation: Ab is "A bar", "AA" is A computed at twice the force of interest. I am making use of the formulas in "Important formulas" posted on the class web page. Things like A40 and AA40 are read off of the ILT (Illustrative Life Table). iod is i/δ , iiodd is i/δ at twice the force of interest. z975 is the 97.5 th percentile of the normal distribution from the table. Note that the problems are not in order.

De Moivre (Problem 4)

$$\begin{aligned} > \text{AbDem} := (w, x, n, \text{del}) \rightarrow \frac{(1 - \exp(-\text{del} \cdot n))}{\text{del} \cdot (w - x)} \\ & \qquad \qquad \qquad \text{AbDem} := (w, x, n, \text{del}) \rightarrow \frac{1 - e^{-\text{del}n}}{\text{del} (w - x)} \end{aligned} \quad (1)$$

$$\begin{aligned} > \text{ADem} := (w, x, n, \text{del}) \rightarrow \frac{\text{del} \cdot \text{AbDem}(w, x, n, \text{del})}{(\exp(\text{del}) - 1)}; \\ & \qquad \qquad \qquad \text{ADem} := (w, x, n, \text{del}) \rightarrow \frac{\text{del} \text{AbDem}(w, x, n, \text{del})}{e^{\text{del}} - 1} \end{aligned} \quad (2)$$

$$\begin{aligned} > \text{A1} := \text{ADem}(100, 40, 60, .05) \\ & \qquad \qquad \qquad \text{A1} := 0.3088851892 \end{aligned} \quad (3)$$

$$\begin{aligned} > \text{A2} := \text{ADem}(100, 40, 60, .1) \\ & \qquad \qquad \qquad \text{A2} := 0.1580793859 \end{aligned} \quad (4)$$

$$\begin{aligned} > \text{V} := \text{A2} - \text{A1}^2 \\ & \qquad \qquad \qquad \text{V} := 0.06266932579 \end{aligned} \quad (5)$$

$$\begin{aligned} > \text{A1} := \text{AbDem}(100, 40, 60, .05) \\ & \qquad \qquad \qquad \text{A1} := 0.3167376438 \end{aligned} \quad (6)$$

$$\begin{aligned} > \text{A2} := \text{AbDem}(100, 40, 60, .1) \\ & \qquad \qquad \qquad \text{A2} := 0.1662535413 \end{aligned} \quad (7)$$

$$\begin{aligned} > \text{V} := \text{A2} - \text{A1}^2 \\ & \qquad \qquad \qquad \text{V} := 0.0659308063 \end{aligned} \quad (8)$$

Problem 5

$$\begin{aligned} > \text{Abexpn} := (m, n, \text{del}) \rightarrow m \cdot \frac{(1 - \exp(-(\text{del} + m) \cdot n))}{\text{del} + m} \\ & \qquad \qquad \qquad \text{Abexpn} := (m, n, \text{del}) \rightarrow \frac{m (1 - e^{-(\text{del} + m) n})}{\text{del} + m} \end{aligned} \quad (9)$$

$$\begin{aligned} > \text{Abexp} := (m, \text{del}) \rightarrow \frac{m}{m + \text{del}} \\ & \qquad \qquad \qquad \text{Abexp} := (m, \text{del}) \rightarrow \frac{m}{m + \text{del}} \end{aligned} \quad (10)$$

$$\begin{aligned} > \text{V} := \text{Abexp}(.02, .1) - \text{Abexp}(.02, .05)^2 \\ & \qquad \qquad \qquad \text{V} := 0.08503401365 \end{aligned} \quad (11)$$

Problem 2

$$\begin{aligned} > \text{V} := 500^2 \cdot (\text{AA40} - \text{A40}^2) \cdot 100; \text{sig} := \text{sqrt}(\text{V}); m := 500 \cdot 100 \cdot \text{A40} \\ & \qquad \qquad \qquad \text{V} := 5.651464400 \cdot 10^5 \\ & \qquad \qquad \qquad \text{sig} := 751.7622230 \\ & \qquad \qquad \qquad m := 8066.00000 \end{aligned} \quad (12)$$

$$> \text{S} := m + \text{sig} \cdot \text{z975}$$

$$S := 9539.453957 \quad (13)$$

Problem 3

$$> V := 500^2 \cdot (iiodd \cdot AA40 - (iod)^2 \cdot A40^2) \cdot 100; sig := \text{sqrt}(V); m := 500 \cdot 100 \cdot A40 \cdot iod$$

$$V := 5.995894465 \cdot 10^5$$

$$sig := 774.3316127$$

$$m := 8305.630150$$

(14)

$$> S := m + sig \cdot z975$$

$$S := 9823.320111$$

(15)