## Topic: Callable Bonds

Ally buys a 10 year callable bond. The bond matures at the end of 10 years for 10,000 . The bond has semi-annual coupons at a rate of $7.5 \%$ convertible semi-annually.

The bond can be called at the end of 5 years for a call value of 10,225 .
The bond can be called at the end of 7 years for a call value of 10,125 .
The bond can be called at the end of 9 years for a call value of 10,050 .
The bond is purchased to yield $7 \%$ convertible semi-annually.
Determine the price of the bond.

## Solution:

Calculate the value at each call date and the maturity date and select the lowest price.

| N | $\mathrm{I} / \mathrm{Y}$ | PMT | FV | CPT PV |
| :---: | :---: | :---: | :---: | :---: |
| 10 | 3.5 | $(10,000)(0.0375)=375$ | 10,225 | $10,367.42$ |
| 14 | 3.5 | 375 | 10,125 | $10,350.24$ |
| 18 | 3.5 | 375 | 10,050 | $10,356.66$ |
| 20 | 3.5 | 375 | 10,000 | $10,355.31$ |

The lowest present value is the price $\rightarrow 10,350.24$

The Vinyard Corporation issues a 10 year callable bond. The bond matures for its par value of 10,000. The bond has coupons payable semi-annually at a rate of $7.5 \%$ compounded semi-annually.

The bond is callable at the end of 6 years with a call value of 10,250 .
The bond is callable at the end of 8 years with a call value of 10,125 .
The bond is purchased to yield 6.8\% compounded semi-annually.
Determine the price of the The Vinyard's bond.

## Solution:

| $n$ | I/Y | PMT | FV | CPT PV |
| :---: | :---: | :---: | :---: | :---: |
| $(6)(2)=12$ | $6.8 / 2=3.4$ | $(10,000)(0.075 / 2)=375$ | 10,250 | $10,507.59$ |
| $(8)(2)=16$ | 3.4 | 375 | 10,125 | $10,499.70$ |
| $(10)(2)=20$ | 3.4 | 375 | 10,000 | $10,501.97$ |

Answer is lowest price of $10,499.70$

ROPS Corporation issues a 25 year callable bond with a par and maturity value of 100,000. The bond has semi-annual coupons at a rate of $8 \%$ convertible semi-annually.

The bond is callable at the end of 10 years. The call value at the end of 10 years is 119,500 .
The bond is callable at the end of 15 years. The call value at the end of 15 years is 114,500 .
Calculate the price of this bond to ensure a yield of $6 \%$ convertible semi-annually.

## Solution:

| $\mathbf{N}$ | $\mathbf{I} / \mathbf{Y}$ | PMT | FV | CPT PV |
| :---: | :---: | :---: | :---: | :---: |
| $(10)(2)=20$ | $6 \% / 2=3$ | $(100,000)(0.08 / 2)=4000$ | 119,500 | $125,674.15$ |
| $(15)(2)=30$ | 3 | 4000 | 114,500 | $125,574.25$ |
| $(25)(2)=50$ | 3 | 4000 | 100,000 | $125,729.76$ |

We select the lowest price so Price $=\mathbf{1 2 5 , 5 7 4 . 2 5}$

A callable bond matures at the end of 20 years for 10,000 . The bond pays coupons at a rate of $7 \%$ convertible semi-annually.

The bond can be called at the end of 14 year for a call value of 10,500 . The bond can be called at the end of 16 years for a call value of 10,350 . Finally, the bond can be called at the end of 18 years for a call value of 10,200 .

Determine the price of this callable bond to yield a return of 7\% convertible semi-annually.

## Solution:

| $\mathbf{I} / \mathbf{Y}$ | $\mathbf{N}$ | FV | PMT | CPT PV |
| :---: | :---: | :---: | :---: | :---: |
| $7 / 2=3.5$ | $14^{*} 2=28$ | 10,500 | $(10,000)(0.07 / 2)=350$ | $10,190.83$ |
| 3.5 | 32 | 10,350 | 350 | $10,116.41$ |
| 3.5 | 36 | 10,200 | 350 | $10,057.97$ |
| 3.5 | 40 | 10,000 | 350 | $10,000.00$ |

Price is 10,000 since that is the lowest price.

A callable bond matures at the end of 20 years for its par value of 10,000 . The bond pays coupons at a rate of $7 \%$ convertible semi-annually.

The bond can be called at the end of 14 years for a call value of 10,500 . The bond can be called at the end of 16 years for a call value of 10,350 . Finally, the bond can be called at the end of 18 years for a call value of 10,200 .

Determine the price of this callable bond to yield a return of 6\% convertible semi-annually.

## Solution:

| $\mathbf{N}$ | $\mathbf{I} / \mathbf{Y}$ | PMT | FV | CPT PV |
| :---: | :---: | :---: | :---: | :---: |
| $(14)(2)=28$ | $6 \% / 2=3$ | $(10,000)(0.07 / 2)=350$ | 10,500 | $11,156.74$ |
| $(16)(2)=32$ | 3 | 350 | 10,350 | $11,155.36$ |
| $(18)(2)=36$ | 3 | 350 | 10,200 | $11,160.62$ |
| $(20)(2)=40$ | 3 | 350 | 10,000 | $11,155.74$ |

Price $=\mathbf{1 1 , 1 5 5 . 3 6}$

A 20 year callable bond has a maturity value equal to the par value of 20,000 and semi-annual coupons paid at a coupon rate of $7.5 \%$ convertible semi-annually. The bond may be called at the end of 12 years for a call value of 21,500 . The bond may be called at the end of 15 years for a call value of 20,800 .
Finally, the bond may be called at the end of 18 years for a call value of 20,300 .
Yang purchased the bond at issue to yield $6 \%$ convertible semi-annually.
Determine the price that Yang paid.

## Solution:

Calculate the value at each call date and the maturity date and select the lowest price.

| N | $\mathrm{I} / \mathrm{Y}$ | PMT | FV | CPT PV |
| :---: | :---: | :---: | :---: | :---: |
| 24 | 3 | $(20,000)(0.0375)=750$ | 21,500 | $23,278.23$ |
| 30 | 3 | 750 | 20,800 | $23,269.66$ |
| 36 | 3 | 750 | 20,300 | $23,378.35$ |
| 40 | 3 | 750 | 20,000 | $23,467.22$ |

The lowest present value is the price $\boldsymbol{\rightarrow} 23,269.66$

Jackson purchases a callable bond. The bond matures at the end of 20 years for 52,000 . The bond pays semi-annual coupons of 1300 .

The bond can be called at the end of 14 years. The call value is 54,925 .
The bond can be called at the end of 16 years. The call value is 53,950 .
The bond can be called at the end of 18 years. The call value is 52,975 .

Jackson buys the bond to yield 4\% convertible semi-annually.

Determine the price of the bond.

## Solution:

Calculate the price at each call date and the maturity date and pick the lowest price.

| $I / Y$ | $\leftarrow 4 \% / 2=2 ; P M T$ | $\leftarrow 1300$ |
| :--- | :---: | :---: |
| $N$ | $F V$ | $P V$ |
| 28 | 54,925 | $59,123.20$ |
| 32 | 53,950 | $59,136.50$ |
| 36 | 52,975 | $59,105.07$ |
| 40 | 52,000 | $59,112.42$ |

