## **EXAMPLES OF SECTIONS 3.1**

**Question 1.** Suppose that A is an  $n \times n$  matrix. Show that if there exists a matrix B such that  $BA = I_n$ , then  $AB = I_n$ .

## SOLUTIONS.

1. First note that  $BA = I_n$  implies that B is also an  $n \times n$  matrix. Taking determinant on both sides of  $BA = I_n$  yields

$$|B||A| = |BA| = |I_n| = 1 \Longrightarrow |A| \neq 0.$$

Recall that in class, we proved that this implies A is invertible. Thus there exists  $A^{-1}$  such that  $A^{-1}A = AA^{-1} = I_n$ . Now applying a similar argument we saw in Section 1.5, we have

$$A^{-1} = I_n A^{-1} = BAA^{-1} = BI_n = B.$$

Hence  $AB = AA^{-1} = I_n$ .