Exam 2

1. (10 points) Find the maximum value of the function

 $f(x,y) = 3x^2 - 6x + 3y^2 - 12y + 17$

subject to the constraint $x^2 + y^2 = 5$.

- A. 2
- B. 32
- C. 62
- D. 92
- E. 122

Exam 2

2. (10 points) Compute the area of one leaf of the graph of the polar function

$$r = \sin(3\theta).$$

(Recall that $\sin^2(\theta) = \frac{1 - \cos(2\theta)}{2}$)

- A. $\pi/12$
- B. 1/12
- C. $2\pi/3$
- D. 2/3
- E. $\pi/3$

- **3.** (10 points) Find the volume of the solid bounded by the surfaces $z = \sqrt{x^2 + y^2}$ and z = 2.
 - A. 2π
 - B. $8\pi/3$
 - C. $10\pi/3$
 - D. 4π
 - E. $14\pi/3$

Exam 2

4. (10 points) Compute

 $\int_0^{\sqrt{2}} \int_x^{\sqrt{4-x^2}} \int_0^{\sqrt{4-x^2-y^2}} \sqrt{x^2+y^2+z^2} \, dz \, dy \, dx.$

- A. $\pi/4$
- B. $\pi/2$
- C. π
- D. 2π
- E. 4π

Exam 2

5. (10 points) Suppose a room has temperature

$$T(x, y, z) = x^2 \cos z + xze^y$$

at a point (x, y, z) in the room. Find the unit vector which gives the direction in which T increases most rapidly at the point (1, 0, 0).



6. (10 points) Classify all critical points of the function

$$f(x,y) = 2x^2 + 2yx^2 - y^2.$$

Exam 2

7. (10 points) Let D be the region bounded by the curves $y = \sqrt{x}$ and y = x/2. Write down (but do not evaluate) **two** iterated integrals with **different** orders of integration that can be used to compute

 $\iint_D \sin(xy) \, dA.$



Exam 2

8. (10 points) Compute

$$\int_0^1 \int_0^{2y^{2/3}} x^2 \sqrt{x^3 + y^2} \, dx \, dy.$$



9. (10 points) Write down (but do not evaluate) an iterated integral that gives the value of

$$\iiint_E xyz \, dV$$

where E is the solid in the first octant bounded by $z = \sqrt{y}, z = x - 2$ and y = 4.



Exam 2

10. Consider the vector field

$$\mathbf{F}(x,y) = \langle 2x, x+y \rangle.$$

(a) (4 points) Sketch the vectors $\mathbf{F}(x, y)$ at each point depicted on the graph below. Draw directly on the graph.



(b) (6 points) Compute $\int_C \mathbf{F} \cdot d\mathbf{r}$ where C is the line segment from (1,1) to (3,2).