

Quiz 3

Problem. Is there a subset of \mathbb{R} with exactly 2016 limit points?

Solution. Yes, we will give an example.

First, recall from lecture that the set

$$E := \left\{ \frac{1}{n} : n \in \mathbb{N} \right\}$$

has exactly one limit point, namely 0. Therefore for any integer k , the set

$$E_k := \left\{ k + \frac{1}{n} : n \in \mathbb{N} \right\}$$

still has one limit point, k .

Our set will be

$$\bigcup_{i=1}^{2016} E_i$$

whose limit points are exactly the set $\{1, 2, \dots, 2016\}$.