

ReVAR: A data-driven algorithm for generating aero-optic phase screens

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Light Detection and Transmission from an Aircraft

Goal: *Detect and transmit* light from the side of a high-speed aircraft.



<https://aero-optics.nd.edu/research/hemispherical-turret-beam-directors/>



[1] E. J. Jumper, S. Gordeyev, and M. R. Whiteley, "Aero-optical effects," in *Aero-Optical Effects*, (John Wiley Sons, Incorporated, United States, 2023).

Light Detection and Transmission from an Aircraft

Goal: *Detect and transmit* light from the side of a high-speed aircraft.



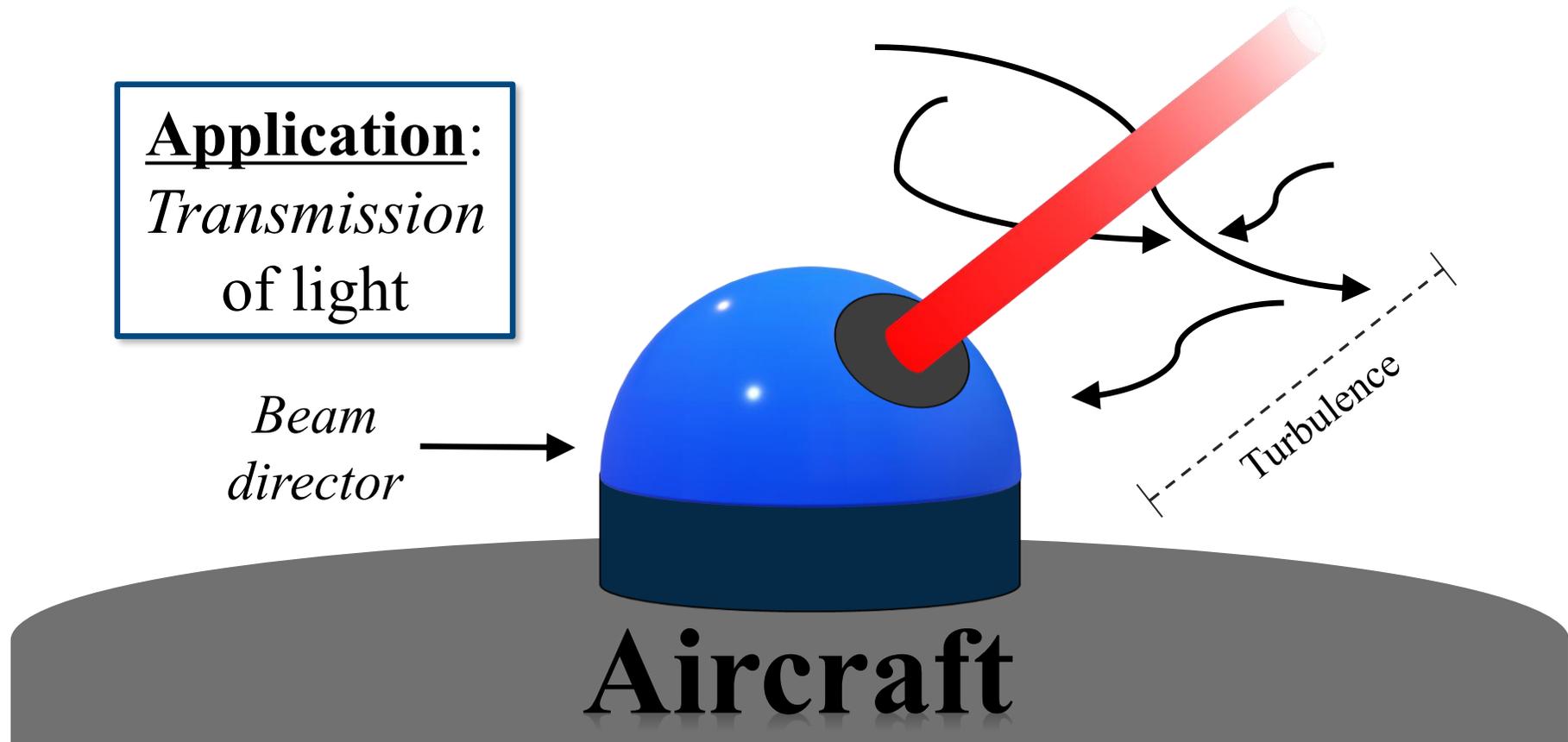
<https://aero-optics.nd.edu/research/aaol/>

Turbulence Near the Aircraft

Problem: Light passes through turbulence *near* the aircraft.

Application:
Transmission
of light

Beam
director



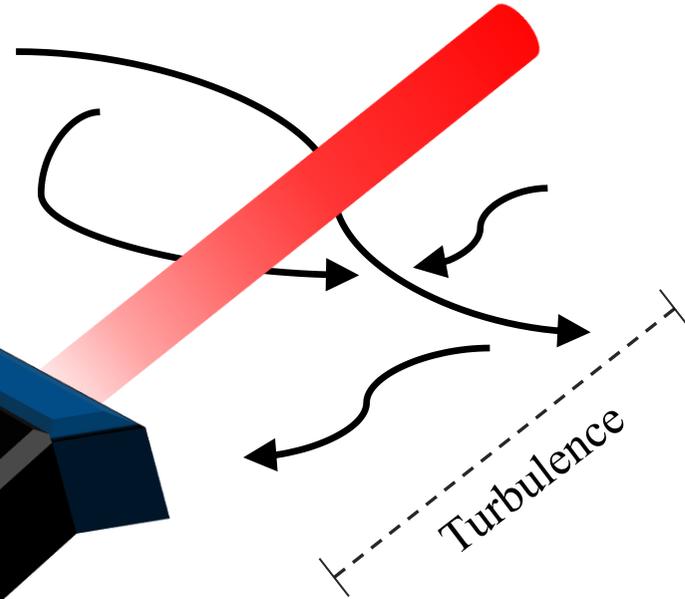
Turbulence Near the Aircraft

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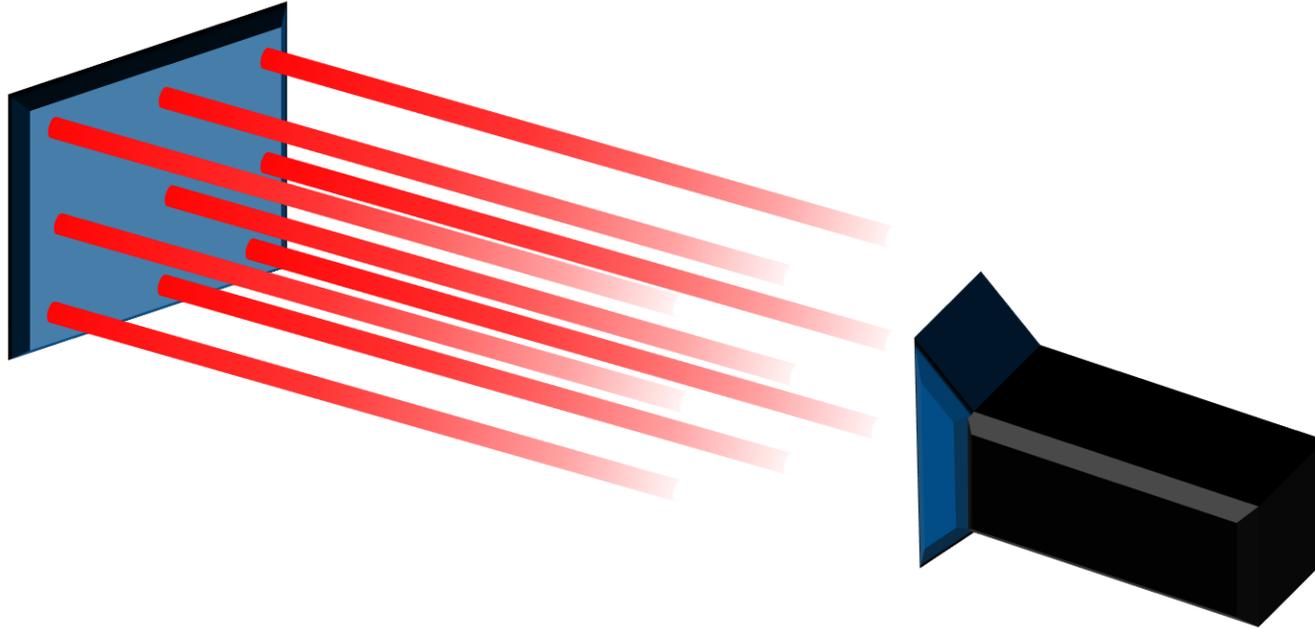
Application:
Detection
of light

Receiver →

Aircraft



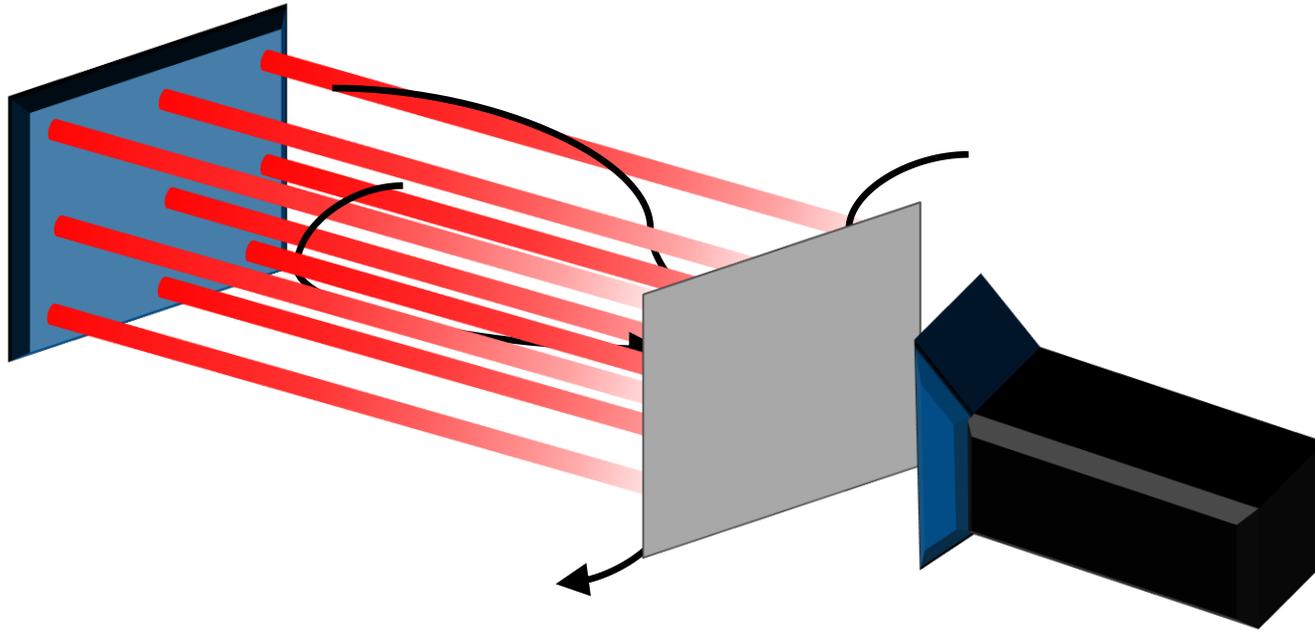
Effect of Turbulence on Light: Aero-Optic Effects



Receiver/target

Without turbulence, light moves
uniformly.

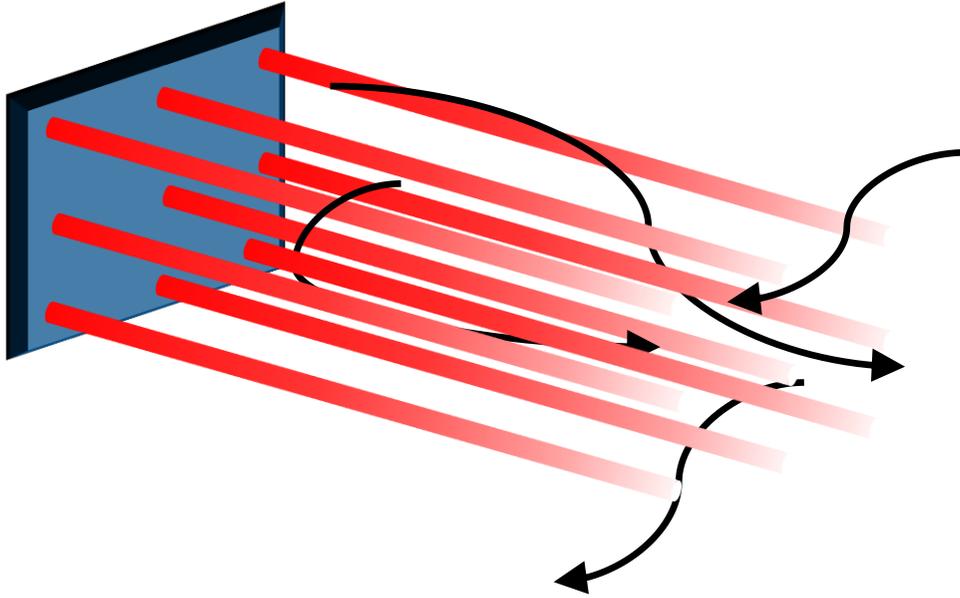
Effect of Turbulence on Light: Aero-Optic Effects



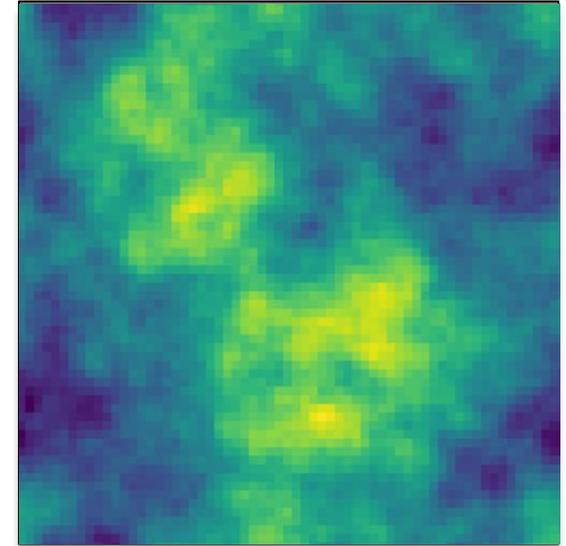
Receiver/target

Velocity changes result in **phase aberrations** in detected light.

Measuring Aero-Optic Effects: Phase Screens



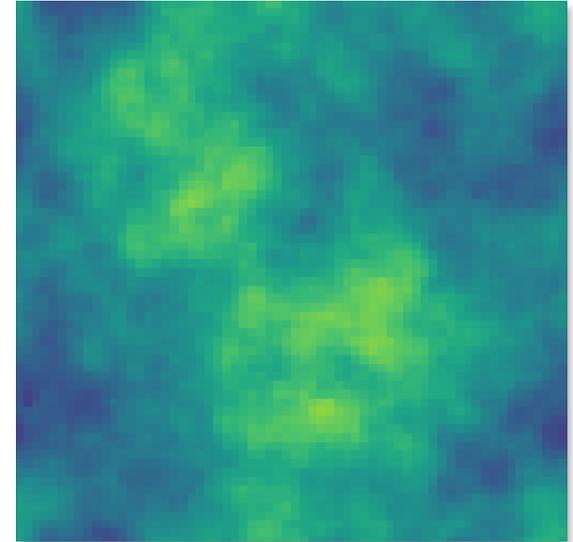
Velocity changes result in **phase aberrations** in detected light.



Phase screens *measure* and *simulate* these phase aberrations.

Measuring Aero-Optic Effects: Phase Screens

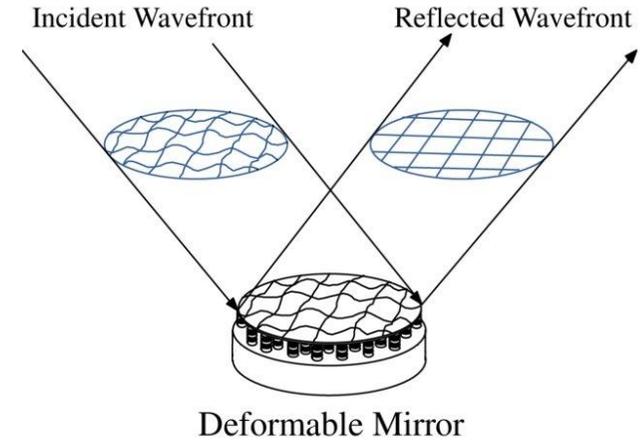
- In addition to *spatial non-uniformity*, these phase aberrations **vary in time**.
- *Time series* of phase screens **capture** this temporal variation.
- These time series *measure* *aero-optic effects*, giving us **aero-optic data**.



Phase screens *measure* and *simulate* these phase aberrations.

We Need Aero-Optic Data!

➤ **Adaptive-optic (AO)** systems can *compensate* for phase aberrations.



- **Problem**: To address aero-optic effects, more sophisticated AO systems must be developed.
- This development *requires aero-optic data*.

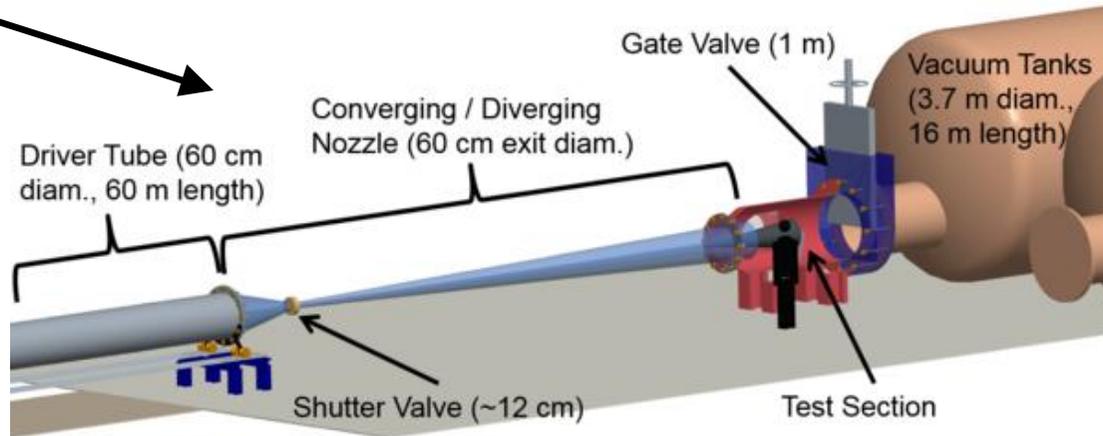
[2] Steinbock, M. J. (2012). *Implementation of branch-point-tolerant wavefront reconstructor for strong turbulence compensation* (No. AFITGEENG1245).

Measuring Aero-Optic Data

Physical experiments
are **expensive!**

➤ **Wind tunnel**
experiments are most
common for measuring
this data.

➤ They require a lot of
time and money.



<https://hyperlab.nd.edu/facilities/>

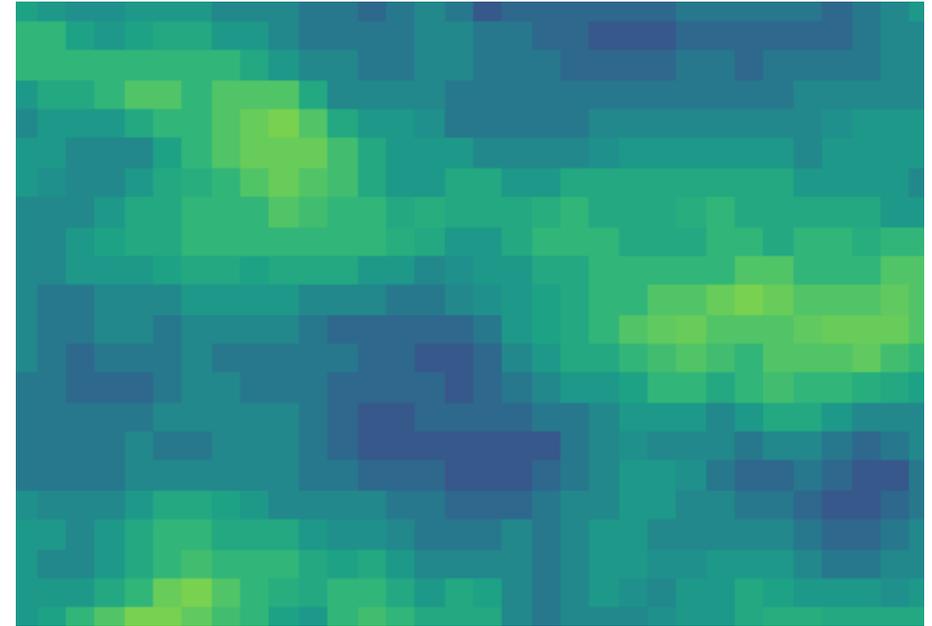
Generating Aero-Optic Data

- Simulations can *generate* this data without the monetary expense of physical experiments.
- As of now, existing simulation methods *still have drawbacks*.
- **Solution**: We develop **ReVAR (Re-whitened Vector Auto-Regression)**, a *data-driven algorithm* that generates *aero-optic data* which match the statistics of measured data.

ReVAR: Re-whitened Vector AutoRegression

ReVAR:

- Take in a **short video** of *measured data*.
- Create a **much longer** video of *synthetic data*.



Match the *spatial* and *temporal* statistics of the measured data.

Presentation Outline

1. Measured Data Sets

2. ReVAR

3. Results

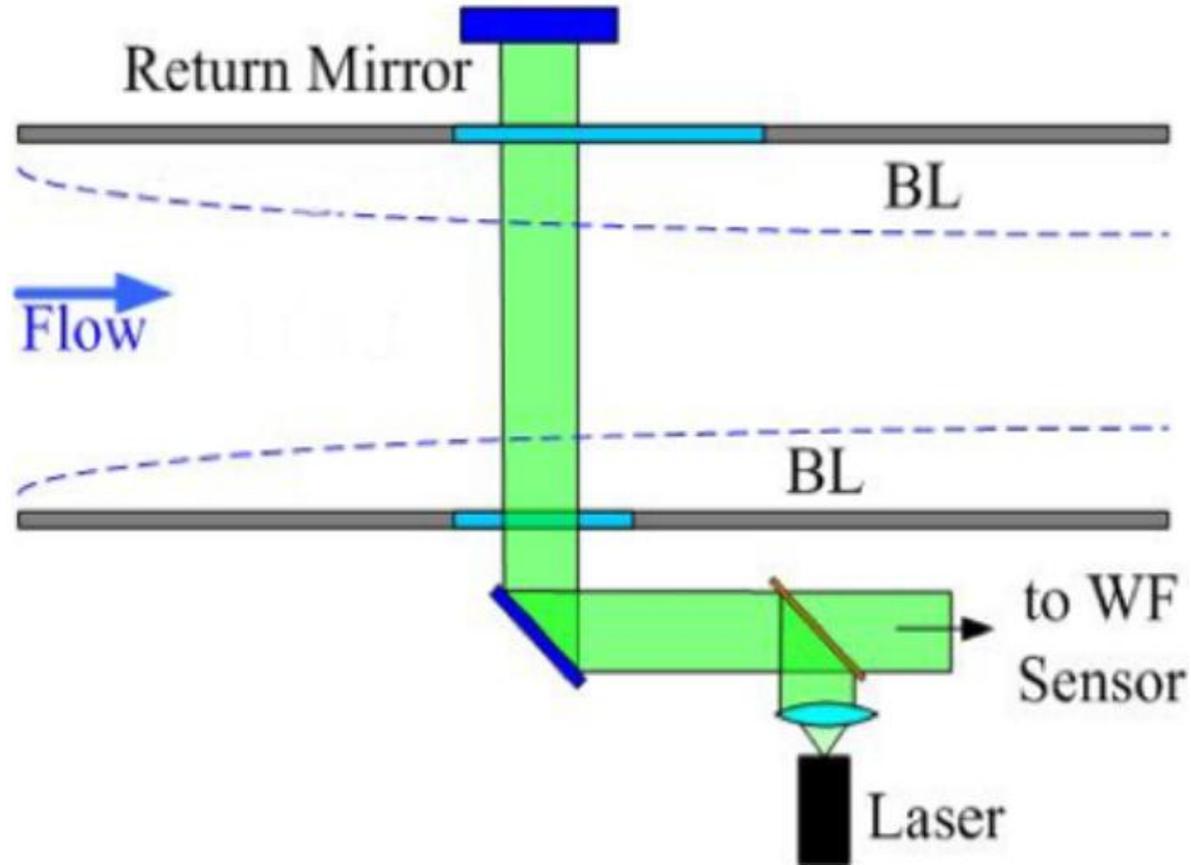
Presentation Outline

1. **Measured Data Sets**

2. ReVAR

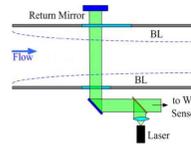
3. Results

Measured Data: Wind Tunnel Experiment

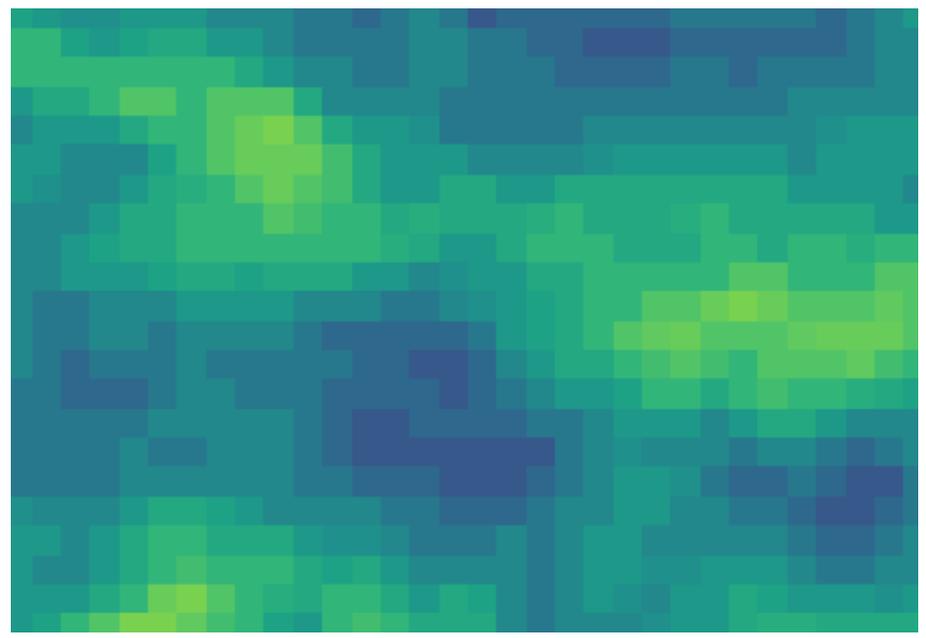


[3] M. R. Kemnetz and S. Gordeyev, "Optical investigation of large-scale boundary-layer structures", *54th AIAA Aerospace Sciences Meeting*, 4 - 8 Jan 2016, San Diego, California, AIAA Paper 2016-1460.

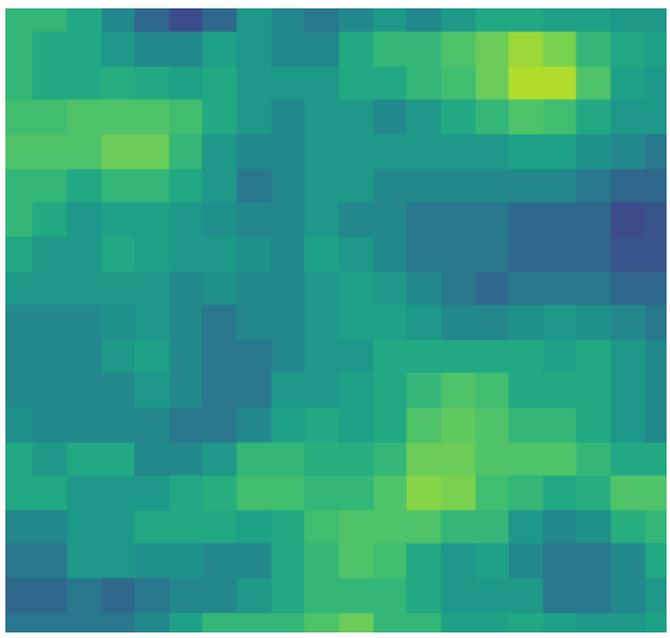
Measured Data: Wind Tunnel Experiment



Dataset 1



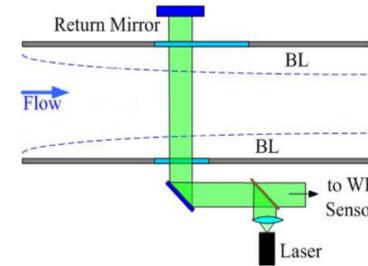
Dataset 2



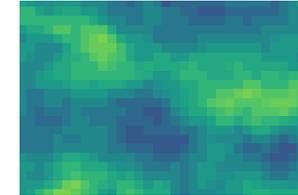
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Presentation Outline

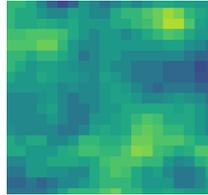
1. Measured Data Sets



Dataset 1



Dataset 2

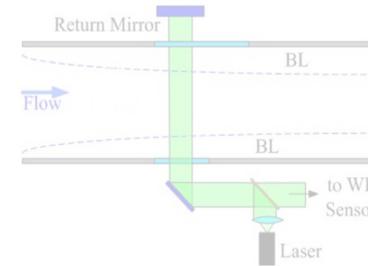


2. ReVAR

3. Results

Presentation Outline

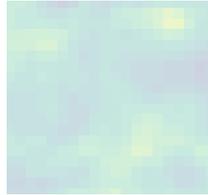
1. Measured Data Sets



Dataset 1



Dataset 2

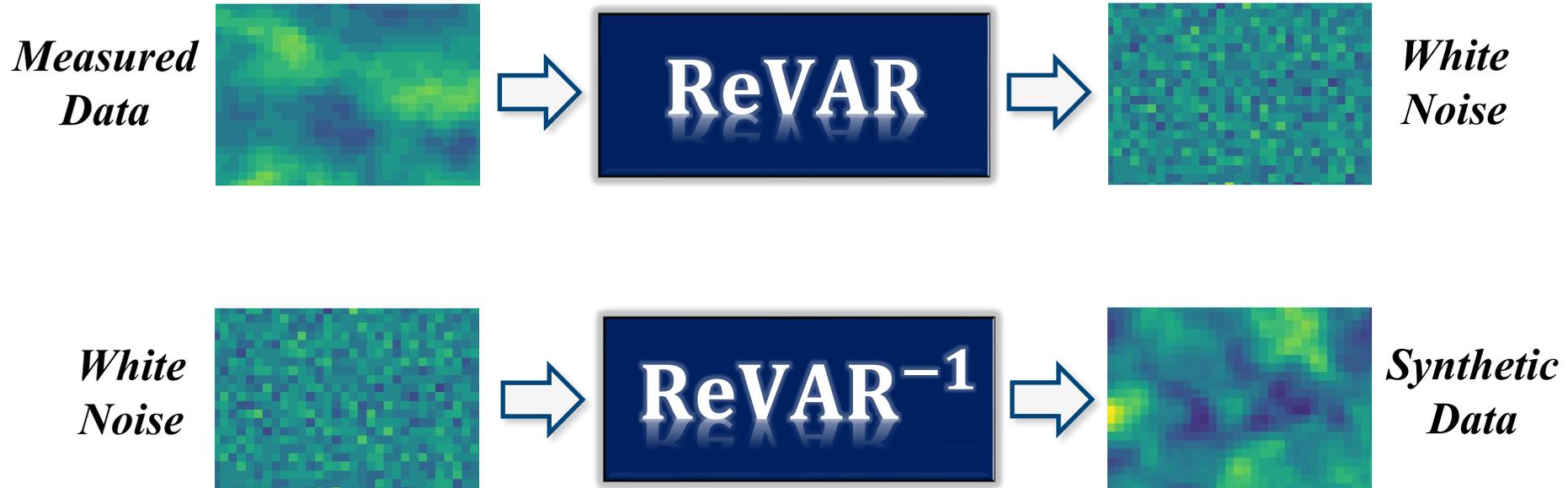


2. **ReVAR**

3. Results

ReVAR: Re-whitened Vector AutoRegression

Transform input data into **white noise** in a way that is **invertible**.



ReVAR: Re-whitened Vector AutoRegression

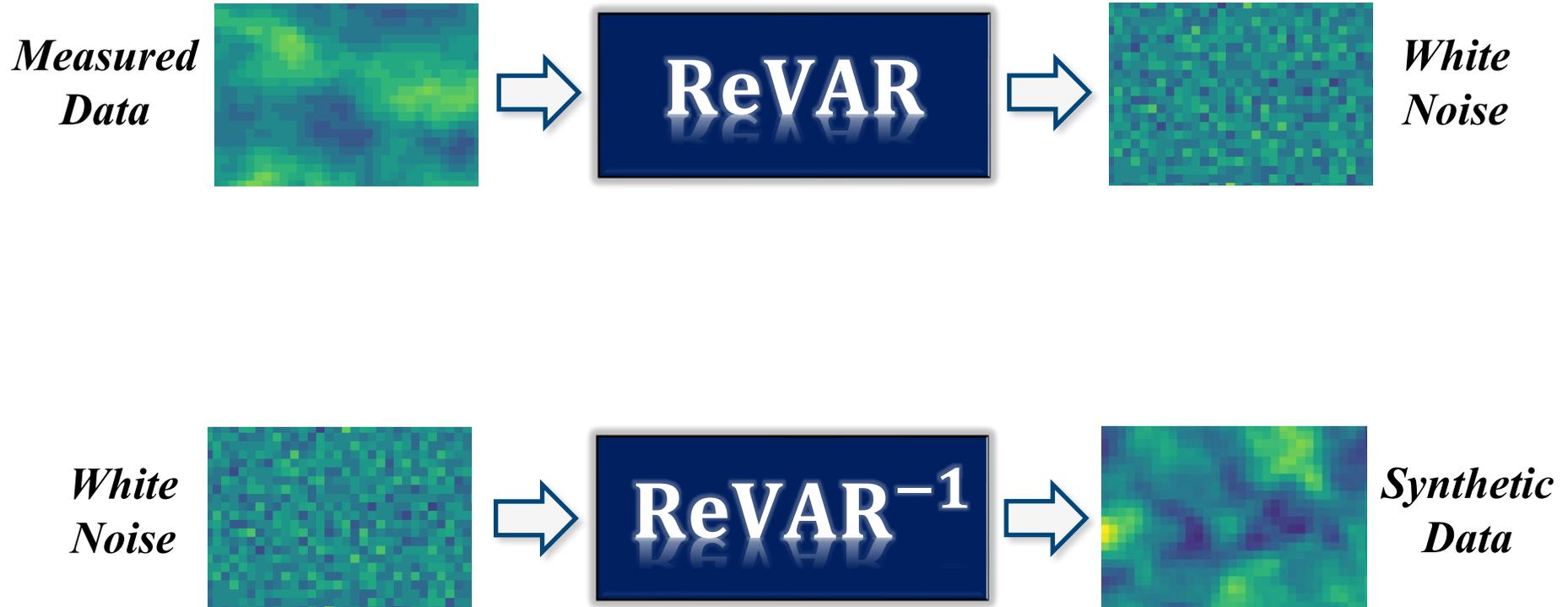
1. Parameter Estimation



2. Data Synthesis



ReVAR: Re-whitened Vector AutoRegression



ReVAR: Re-whitened Vector AutoRegression

ReVAR

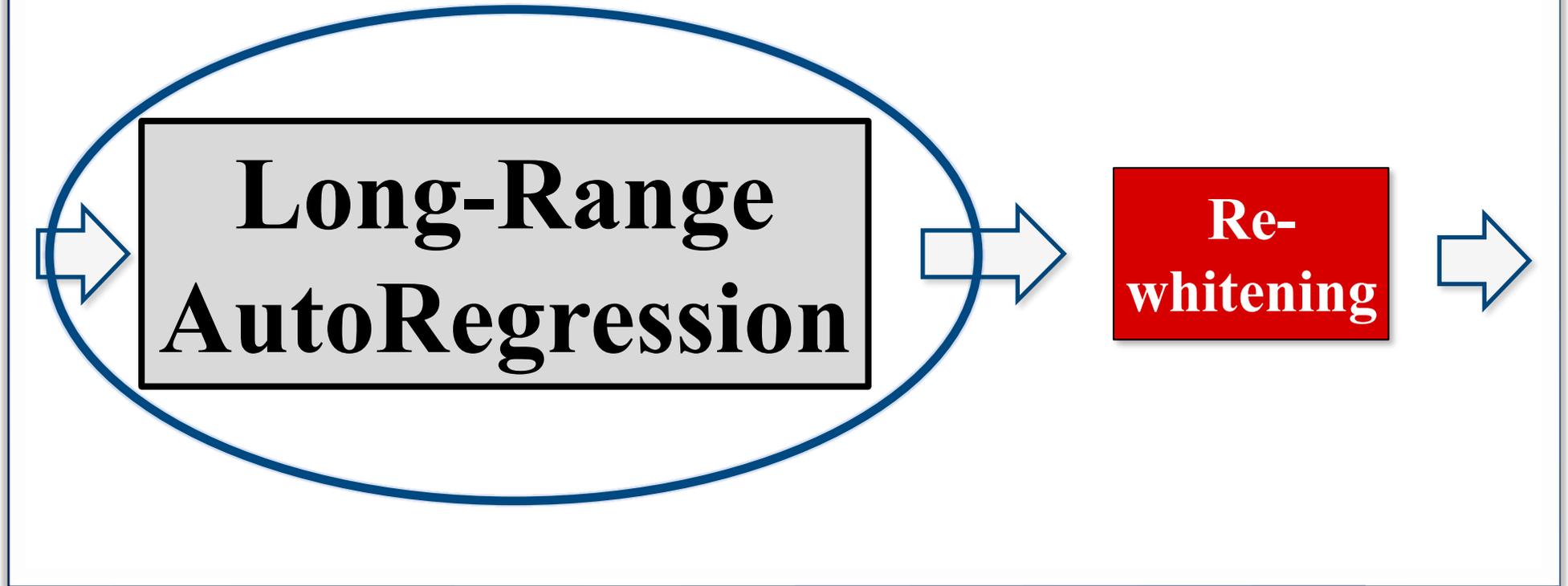
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ReVAR

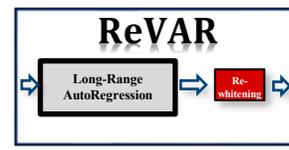


ReVAR: Re-whitened Vector AutoRegression

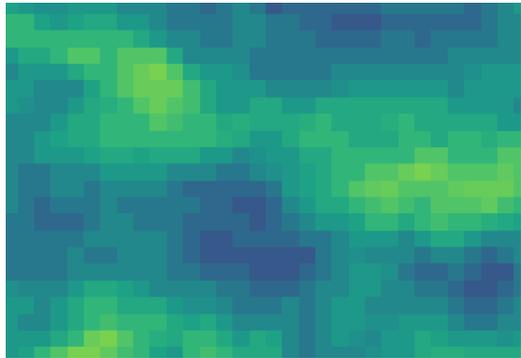
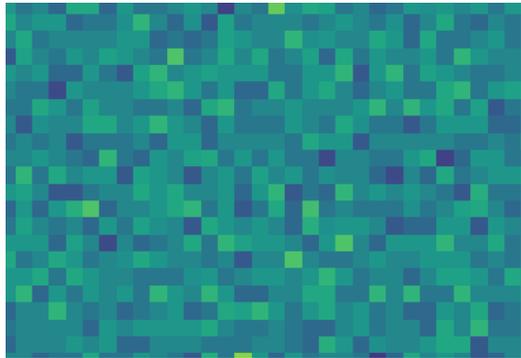
ReVAR



Long-Range AutoRegression



- **Idea:** At each time, represent the data through *some linear prediction* of previous data, plus *some noise*.

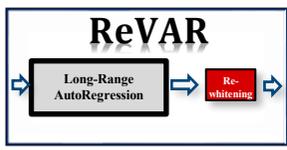
 =  + 

The diagram illustrates the equation: $\text{Noisy Image} = \text{Linear Prediction} + \text{Noisy Image}$. The 'Linear Prediction' is represented by a grey box with a green border containing the text 'Linear Prediction'.

Long-Range AutoRegression

➤ **Idea:** At each time, represent the data through *some linear prediction* of previous data, plus *some noise*.

$$\begin{matrix}
 \text{[Colorful Bar]} & = & \text{[Linear Prediction Box]} & + & \text{[Colorful Bar]} \\
 X_n & = & \hat{X}_n & + & \xi_n
 \end{matrix}$$

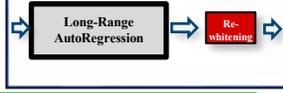


Long-Range AutoRegression

- **Idea:** At each time, represent the data through *some linear prediction* of previous data, plus *some noise*.
- For this linear predictor, we use a *long-range predictor*.

The visual equation shows a vertical bar of data points on the left, followed by an equals sign, a box labeled 'Long-Range Predictor', a plus sign, and another vertical bar of data points on the right. Below this, the mathematical equation is written as $X_n = \hat{X}_n + \xi_n$.

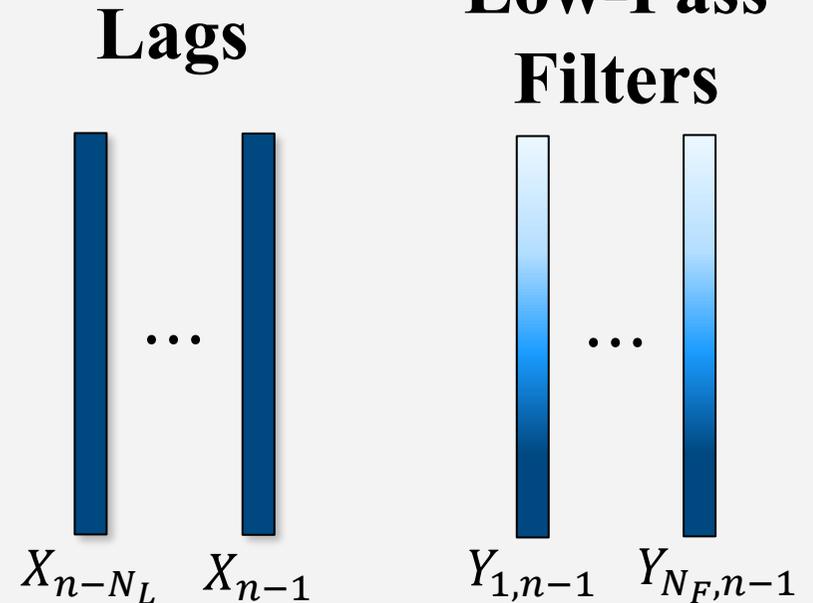
$$X_n = \hat{X}_n + \xi_n$$



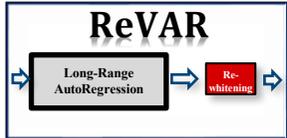
Long-Range Predictor

➤ Send the following *components* into a **linear predictor**:

- 1. Lags:** Most recent time-steps $X_{n-N_L}, \dots, X_{n-1}$.
 - 2. Low-Pass Filters:** A collection of LPFs of the entire time history: $Y_{1,n-1}, \dots, Y_{N_F,n-1}$.
- **(1)** captures *short-range* temporal correlations and **(2)** captures *long-range* correlations.



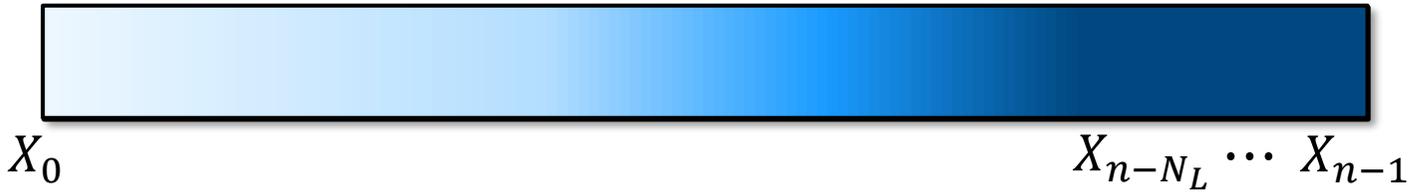
Long-Range Predictor



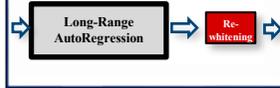
*Low-Pass
Filters*

...
 $Y_{1,n-1} \cdots Y_{N_F,n-1}$

Lags

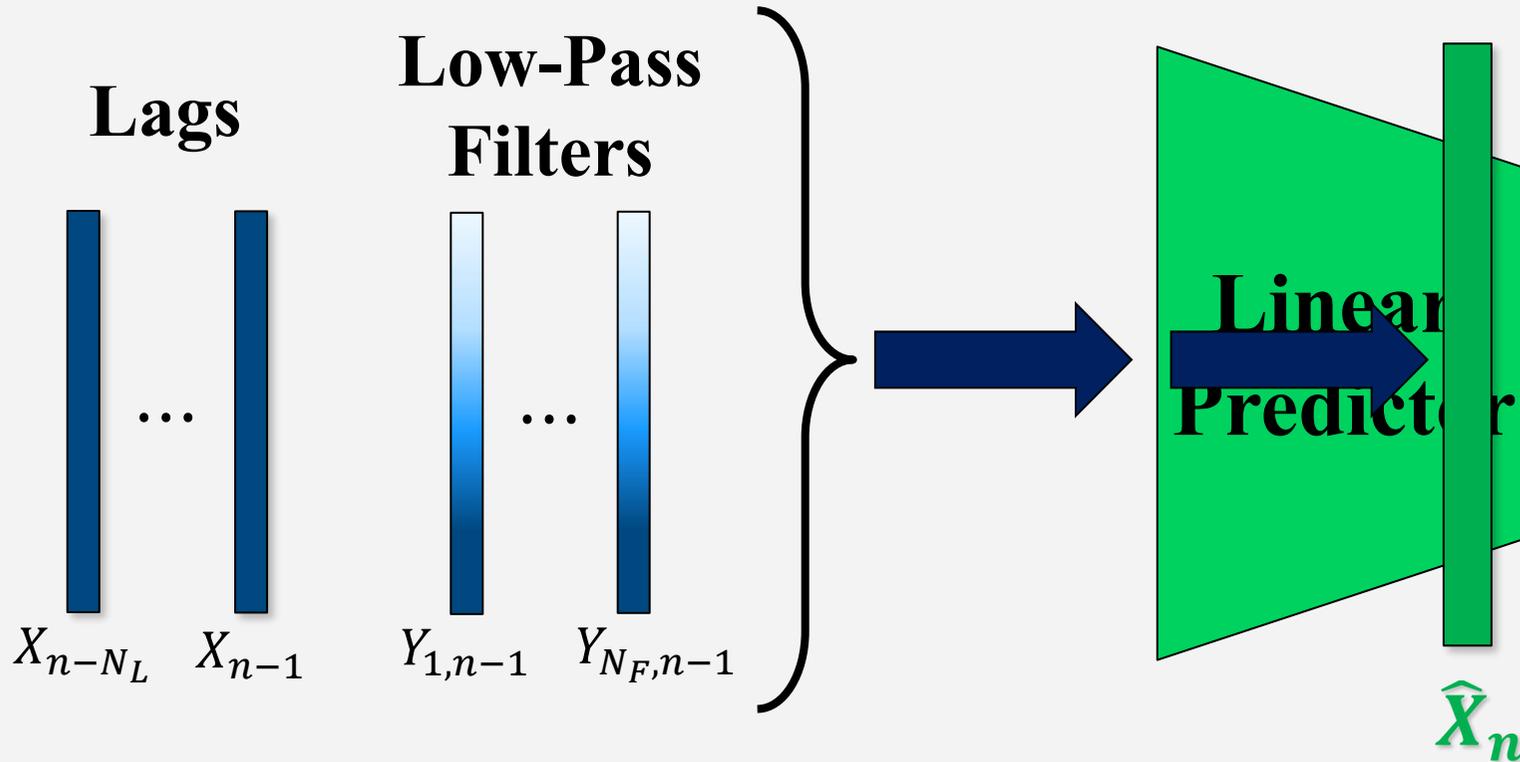


Time History

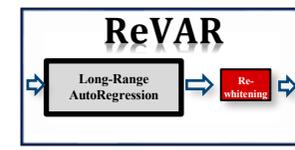


Long-Range Predictor

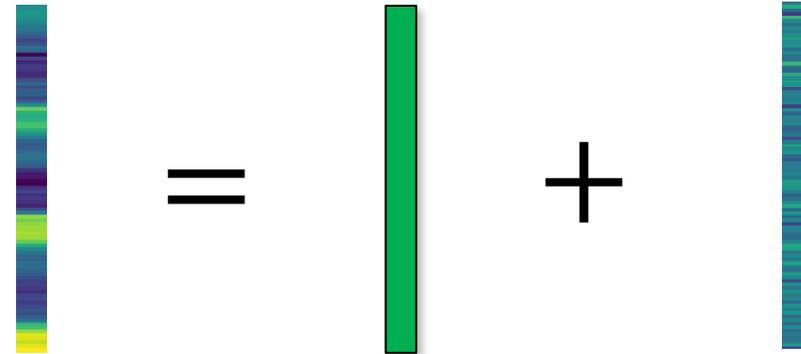
The **linear predictor** determines the next time-step.



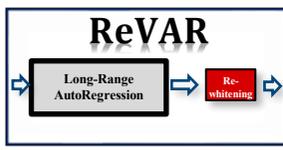
Long-Range AutoRegression



- Long-Range Predictor \hat{X}_n : Use a linear prediction that captures *both* short- and long-range temporal correlations.



$$X_n = \hat{X}_n + \xi_n$$



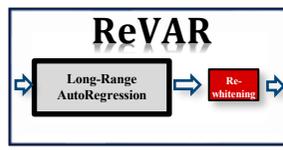
Long-Range AutoRegression

- Long-Range Predictor \hat{X}_n : Use a linear prediction that captures *both* short- and long-range temporal correlations.
- Additive Noise ξ_n : The *residuals* of the long-range predictor.

A visual representation of the equation $\xi_n = X_n - \hat{X}_n$. It consists of three vertical bars: a multi-colored bar on the left, an equals sign, a multi-colored bar in the middle, a minus sign, and a solid green bar on the right. Below these bars, the corresponding mathematical symbols are written in matching colors: a red ξ_n , a blue X_n , a minus sign, and a green \hat{X}_n .

$$\xi_n = X_n - \hat{X}_n$$

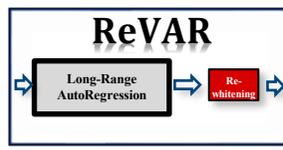
Long-Range AutoRegression



What are the
statistics of the
residuals ξ_n ?

ξ_n

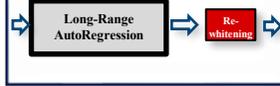
Long-Range AutoRegression



ξ_n

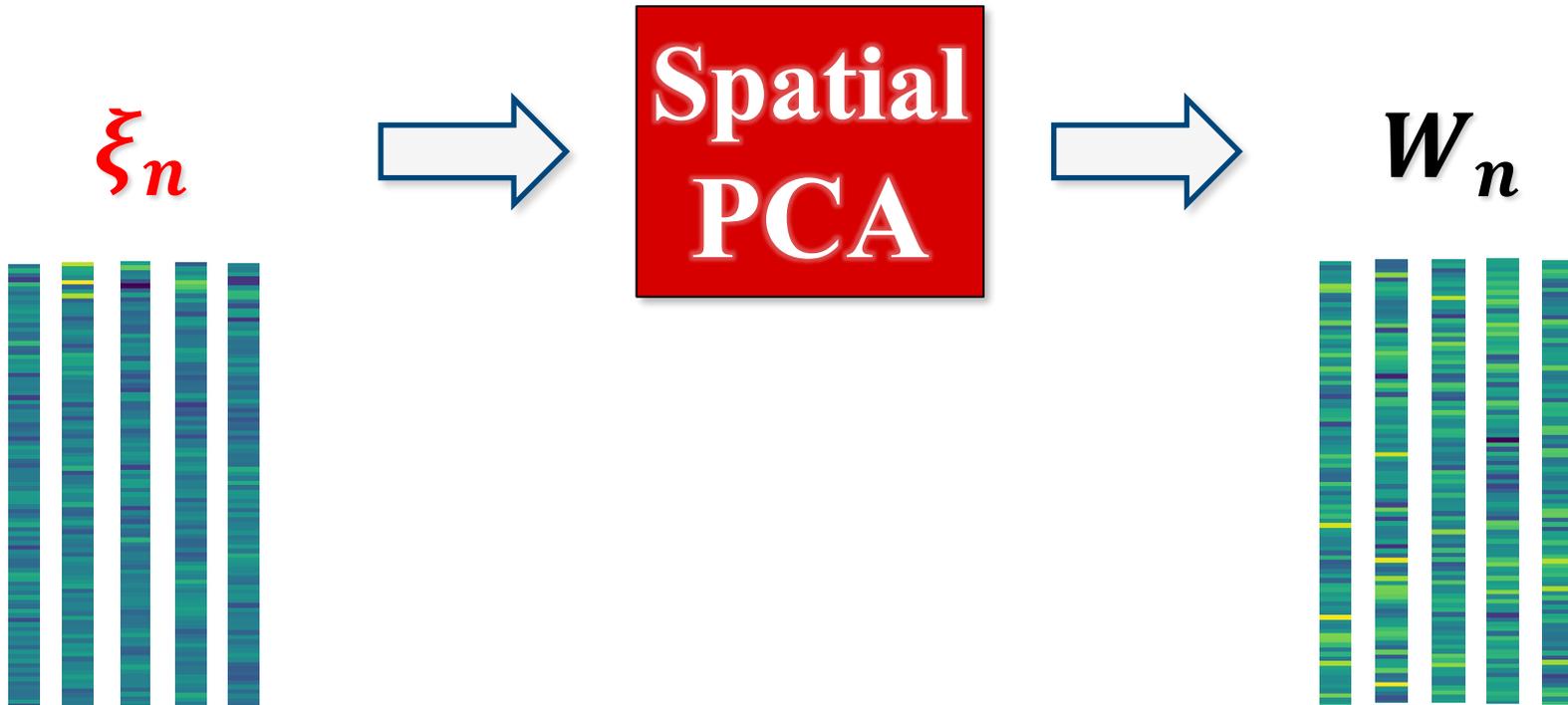
What are the
statistics of the
residuals ξ_n ?

ξ_n is **white** in *time*
but **correlated** in
space.

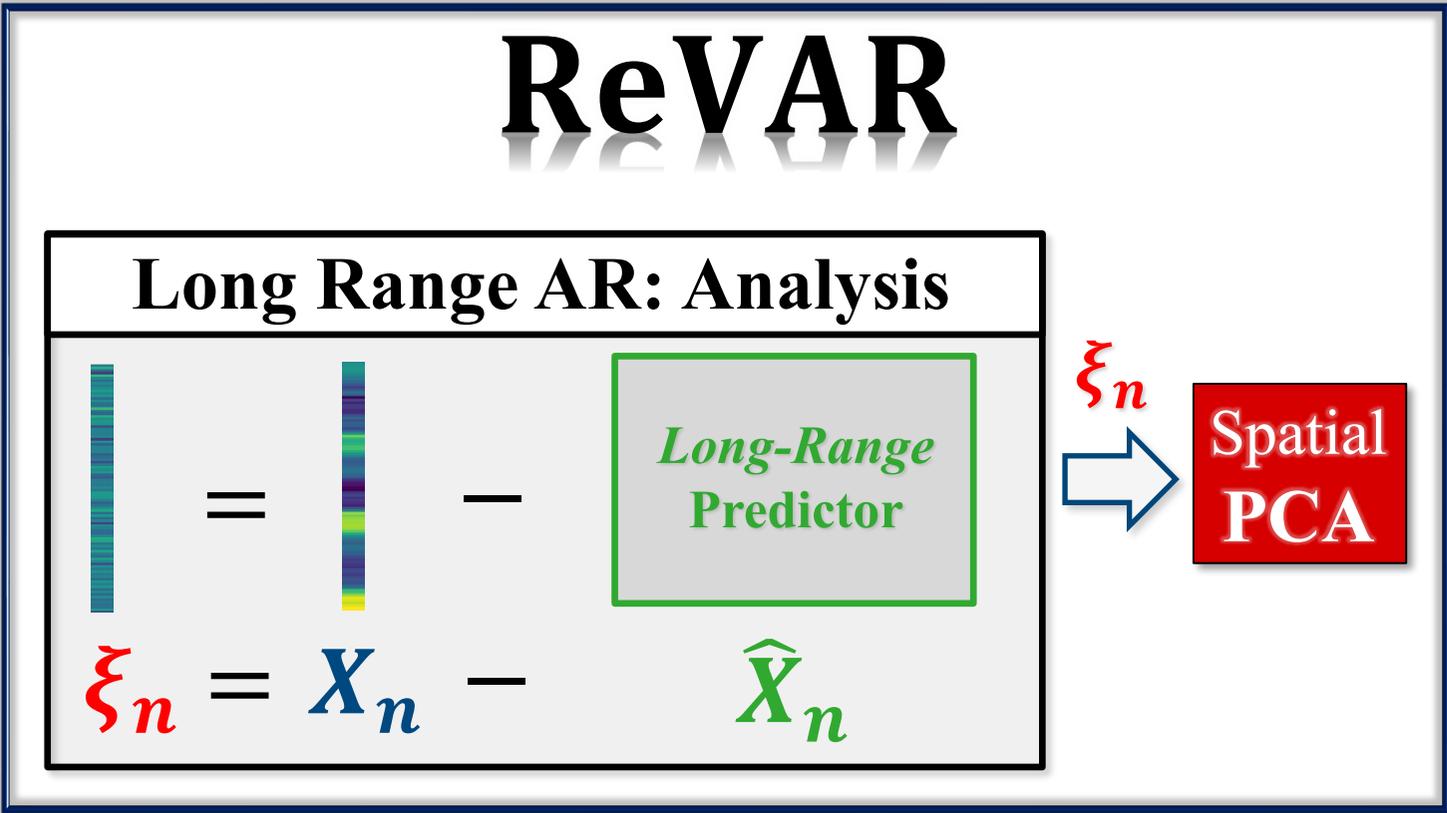


Parameter Estimation: Re-whitening

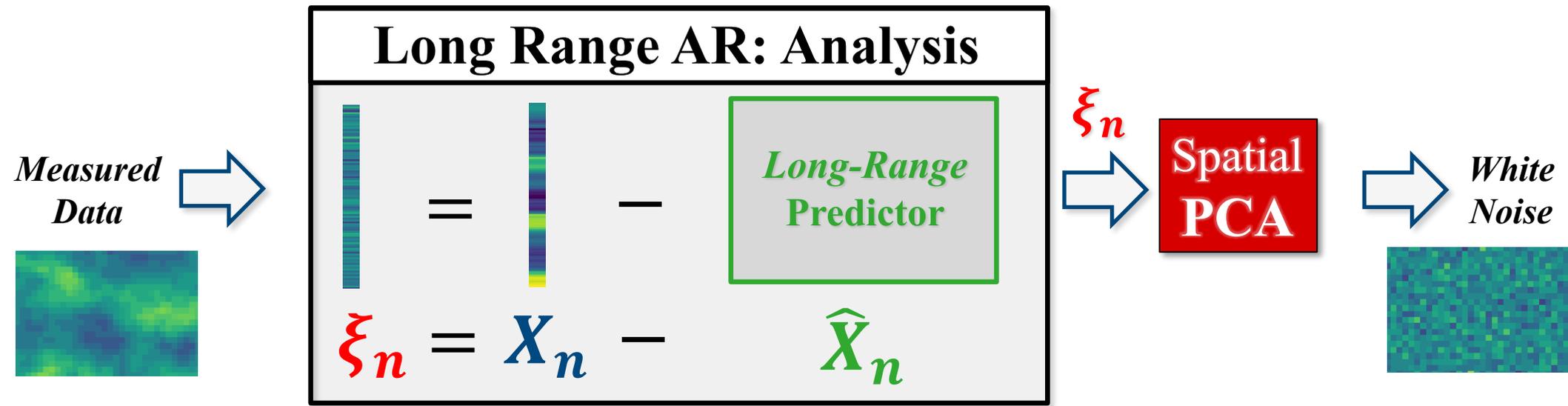
A **spatial PCA** whitens ξ_n in space.



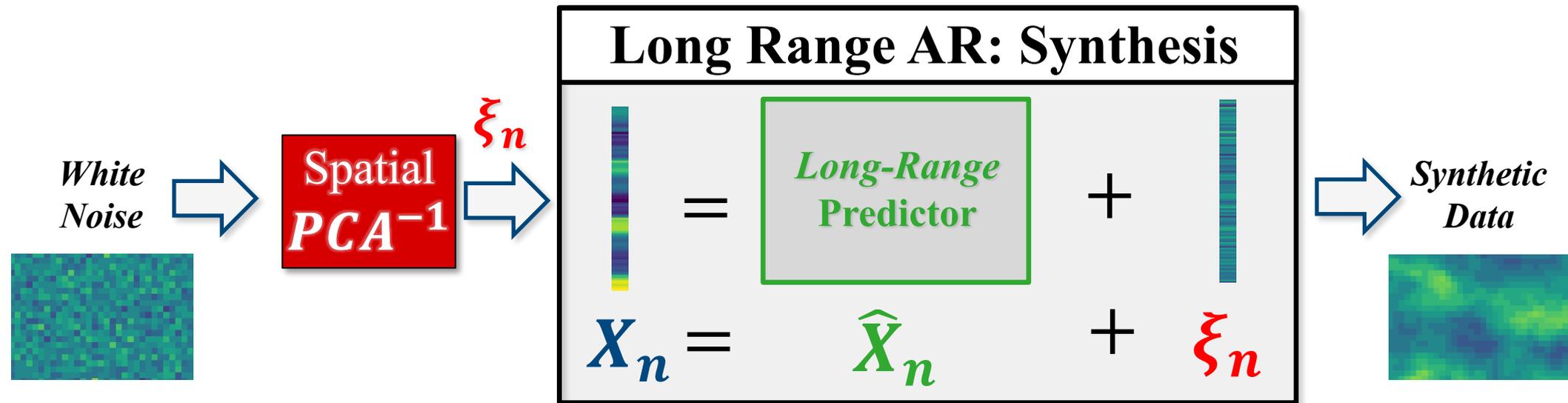
ReVAR: Parameter Estimation



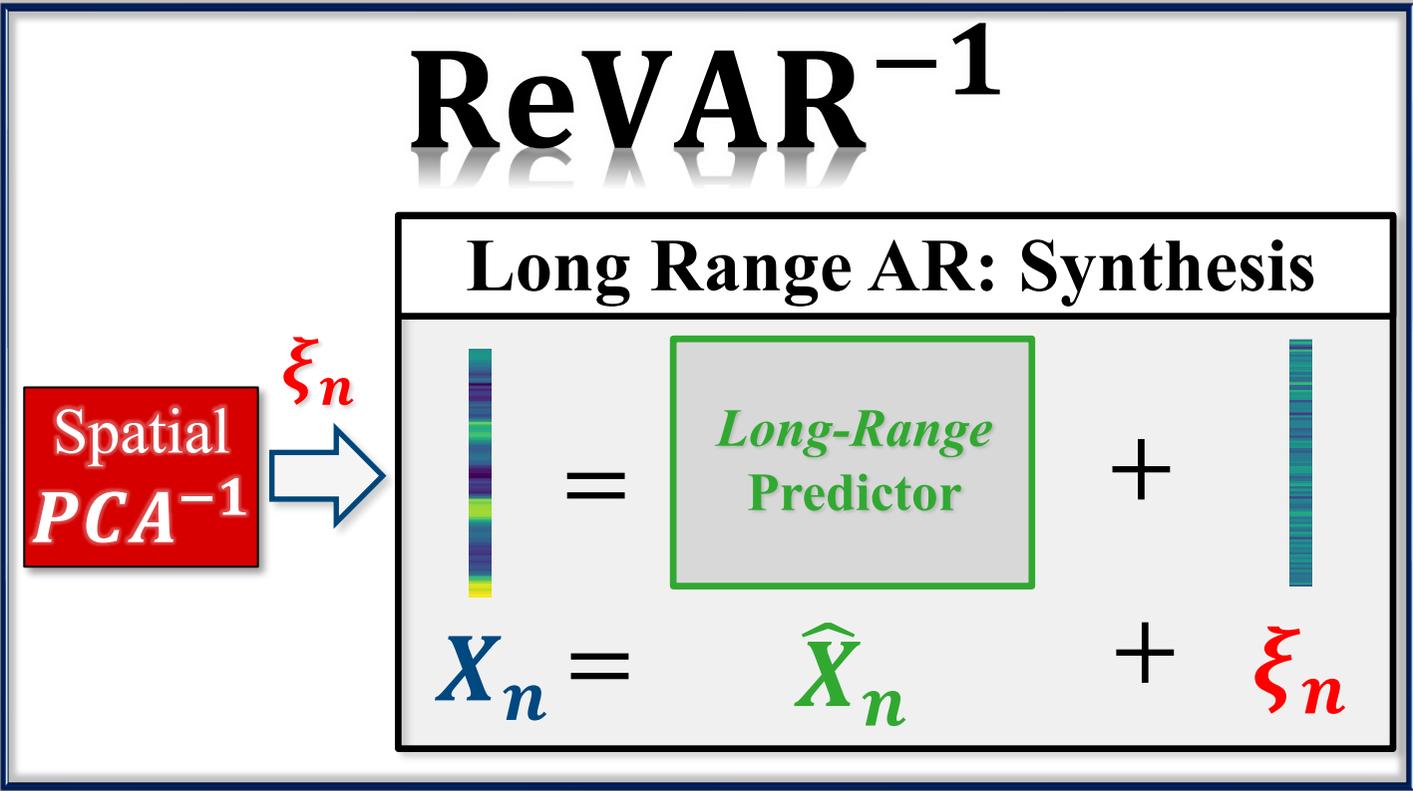
ReVAR: Parameter Estimation



ReVAR: Data Synthesis

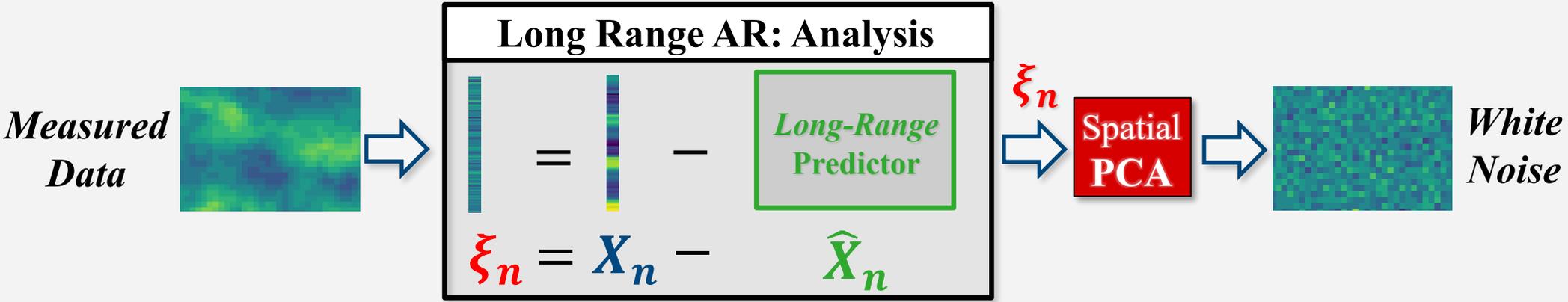


ReVAR: Data Synthesis

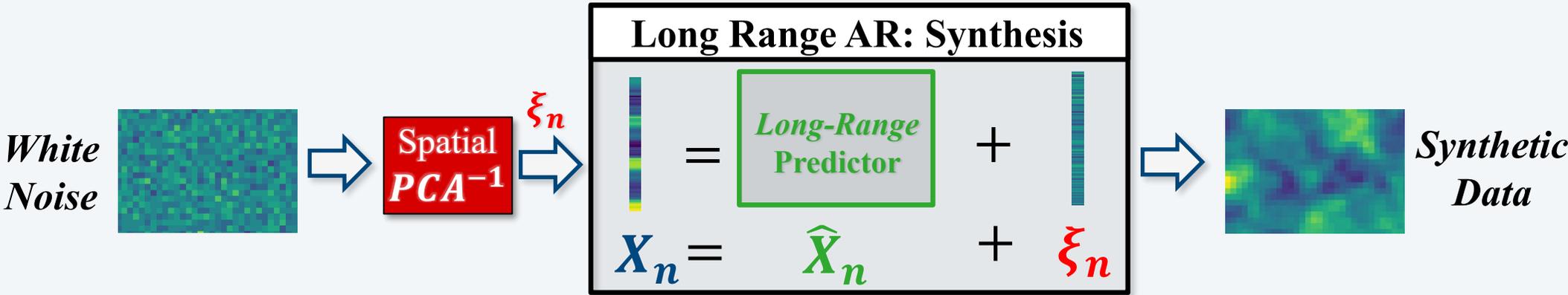


ReVAR: Algorithm Overview

1. Parameter Estimation

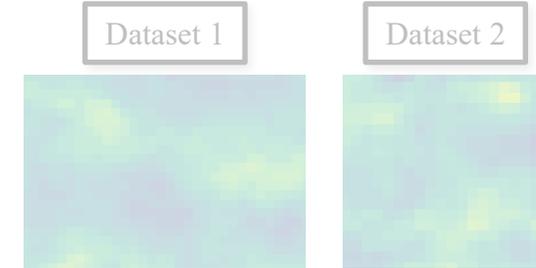
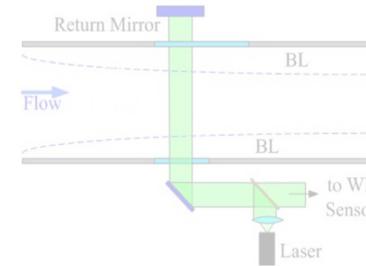


2. Data Synthesis

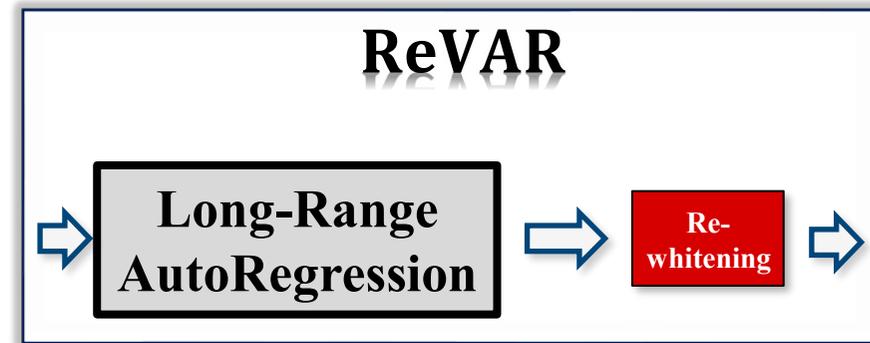


Presentation Outline

1. Measured Data Sets



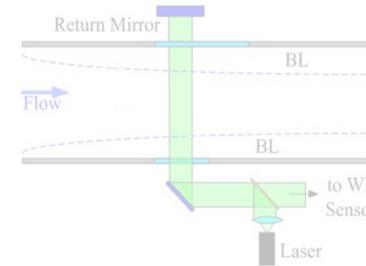
2. ReVAR



3. Results

Presentation Outline

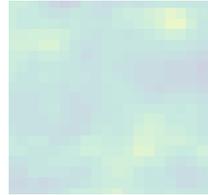
1. Measured Data Sets



Dataset 1



Dataset 2

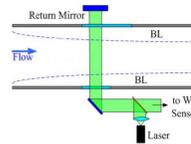


2. ReVAR

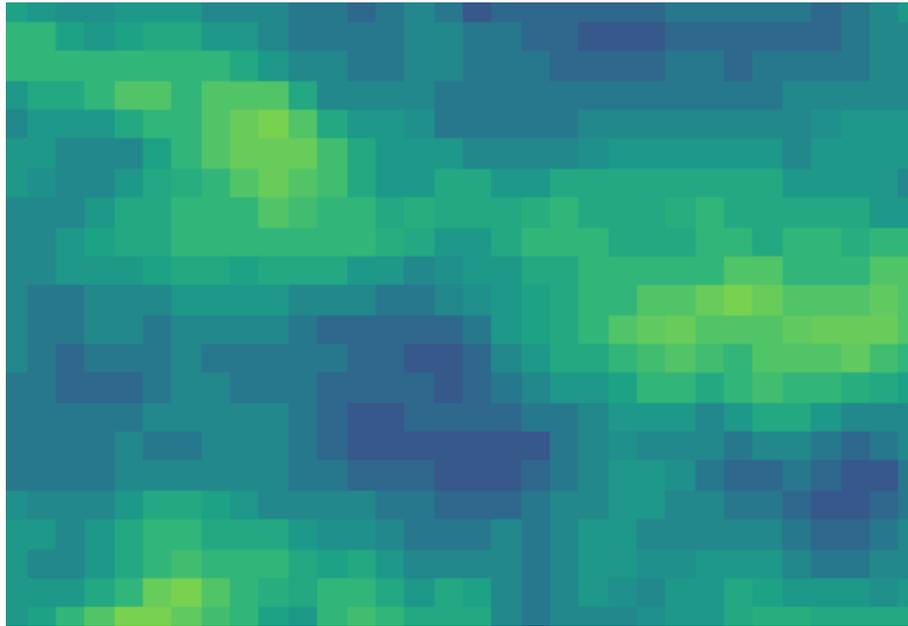


3. Results

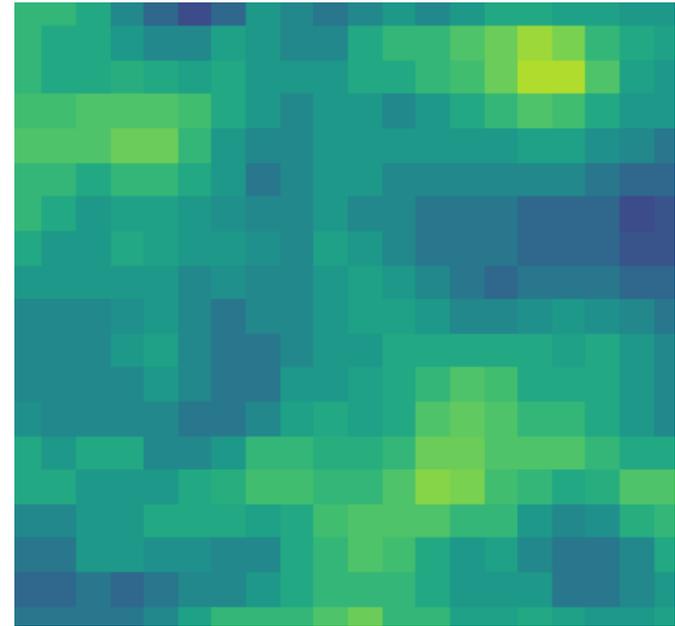
Measured Data: Wind Tunnel Experiment



Dataset 1



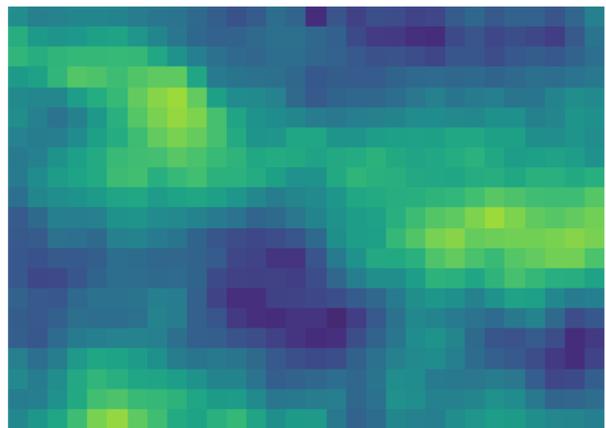
Dataset 2



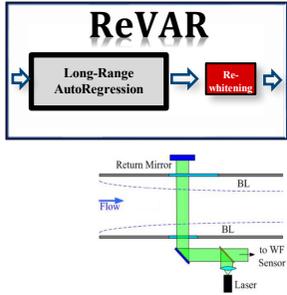
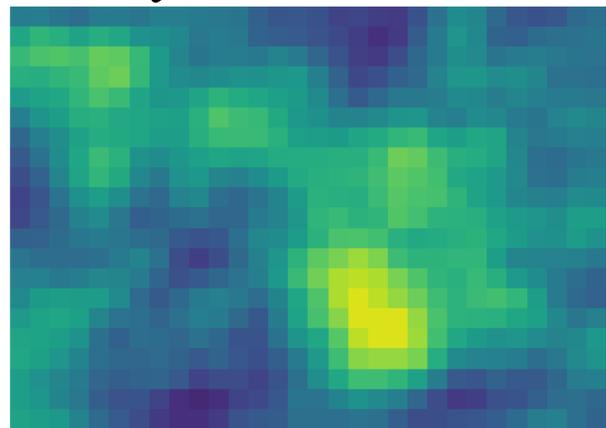
[3] M. R. Kemnetz and S. Gordeyev, "Optical investigation of large-scale boundary-layer structures", *54th AIAA Aerospace Sciences Meeting*, 4 - 8 Jan 2016, San Diego, California, AIAA Paper 2016-1460.

Results: Dataset 1

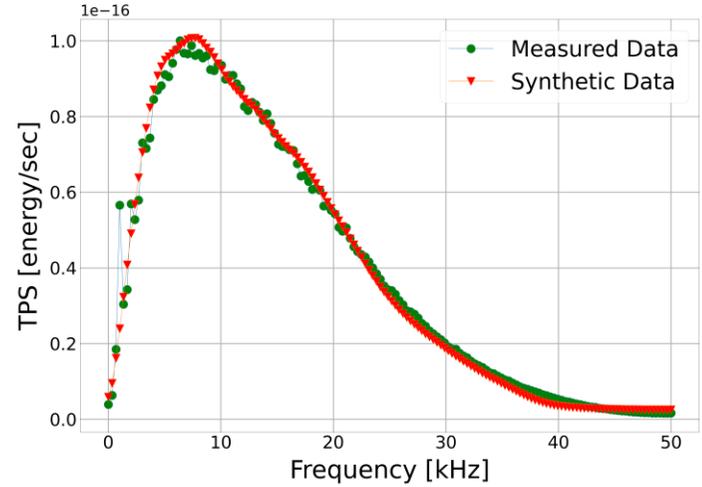
Measured data



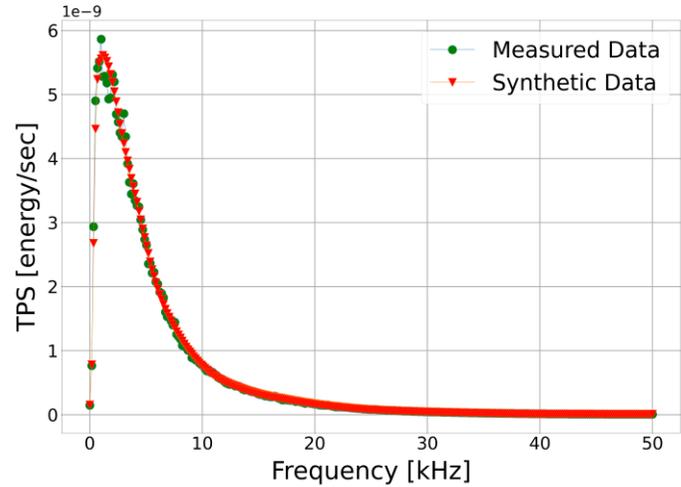
Synthetic data



Temporal Power Spectrum: Streamwise Slopes

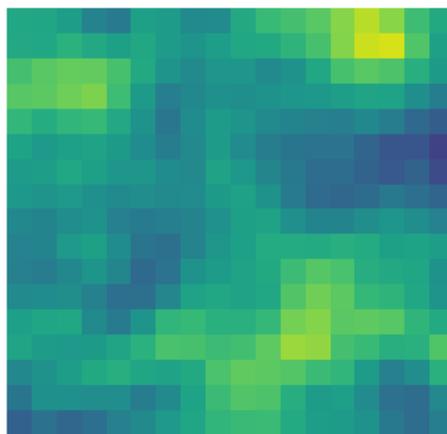


Temporal Power Spectrum: Phase Screens

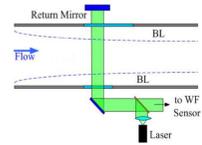
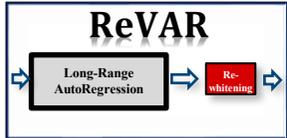
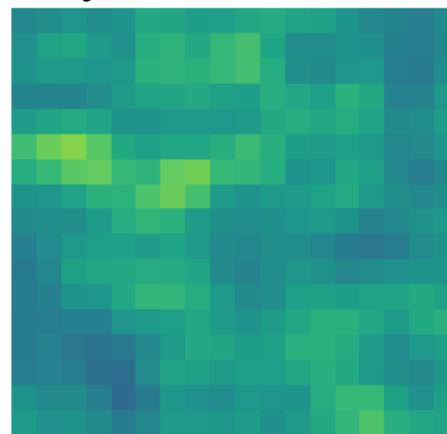


Results: Dataset 2

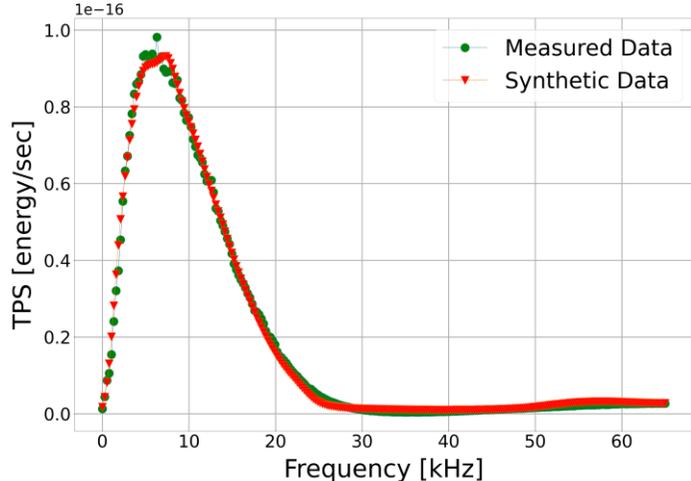
Measured data



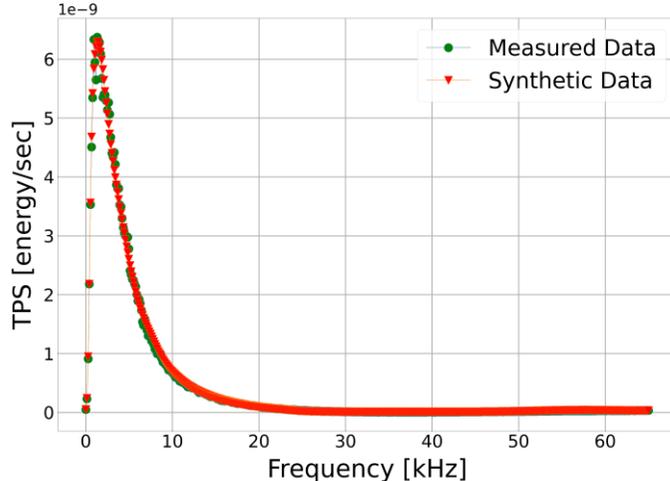
Synthetic data



Temporal Power Spectrum: Streamwise Slopes

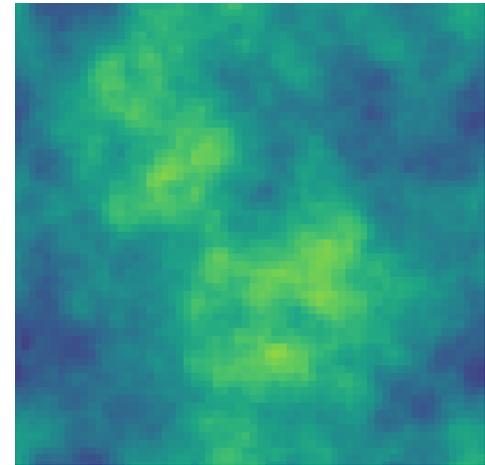
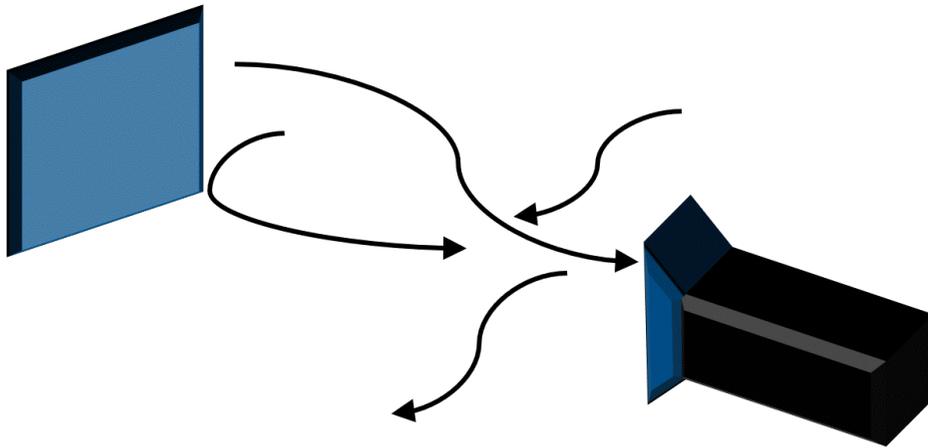


Temporal Power Spectrum: Phase Screens



Summary

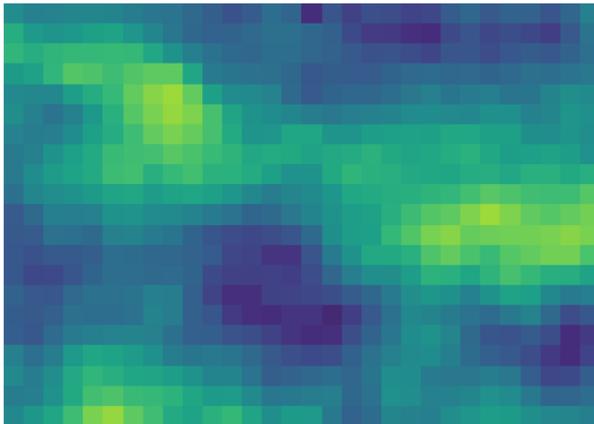
- Aero-optic effects **degrade** imaging and communication **performance** from a high-speed aircraft.
- We **need aero-optic data** to develop AO systems, but *existing* ways of getting this data have *significant drawbacks*.



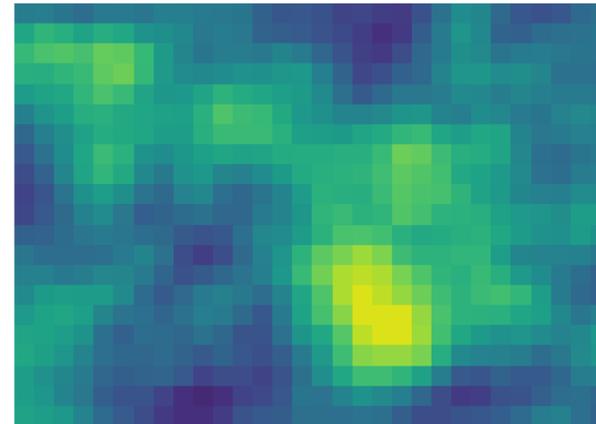
Conclusion

We introduce **ReVAR**: a data-driven algorithm that generates aero-optic data which match the statistics of measured data.

Measured data



Synthetic data



References

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- [2] Steinbock, M. J. (2012). *Implementation of branch-point-tolerant wavefront reconstructor for strong turbulence compensation* (No. AFITGEENG1245)
- [3] M. R. Kemnetz and S. Gordeyev, "Optical investigation of large-scale boundary-layer structures", *54th AIAA Aerospace Sciences Meeting*, 4 - 8 Jan 2016, San Diego, California, AIAA Paper 2016-1460.