## MATH 265 - HANDWRITTEN HOMEWORK 26

- 1. Express the quotient  $z = \frac{1+3i}{6+8i}$  as  $z = re^{i\theta}$ .
- 2. Express  $z = 10e^{i\frac{\pi}{6}}$  as z = a + bi.
- 3. Find all values of r such that the complex number  $re^{i\frac{\pi}{4}}=a+bi$ , where both a and b are integers.
- 4. Find all read and complex roots of the equation  $z^{10} = 9^{10}$ .
- 5. Find all real and complex solutions to the equation  $x^4 2x^2 + 1 = 0$ .
- 6. Find all real and complex eigenvalues of the matrix

$$A = \begin{bmatrix} 4 & 0 & 0 \\ 0 & 1 & -1 \\ 0 & 5 & -3 \end{bmatrix}.$$

- 7. Show that if p(x) is a polynomial with real coefficients and z is a solution of p(x) = 0, then  $\bar{z}$  is also a solution of p(x) = 0, that is  $p(\bar{z}) = 0$ .
- 8. We can associate a complex number and a vector on the plane  $\mathbb{R}^2$  by  $a + bi \equiv \begin{bmatrix} a \\ b \end{bmatrix}$ . Find the matrix  $B = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix}$  such that

$$e^{\mathrm{i}\phi}(a+b\mathrm{i}) \equiv B \begin{bmatrix} a \\ b \end{bmatrix}.$$

And use this to explain geometrically the action of the matrix B on the vector  $\begin{bmatrix} a \\ b \end{bmatrix}$ .