

Amazingly the answer in the back of the book for #7 p. 247 is correct. Here are some hints.

$$Y(s) = \frac{10}{s((s+1)^2+9)} - \frac{10e^{-4s}}{s((s+1)^2+9)} - \frac{10e^{-5s}}{(s+1)^2+9} + \frac{s}{(s+1)^2+9} + \frac{3}{(s+1)^2+9}$$

$$\mathcal{L}^{-1}\left(\frac{10}{s((s+1)^2+9)}\right) = \frac{10}{3} \int_0^t e^{-\tau} \sin 3\tau \, d\tau = \frac{e^{-t}}{3} (-\sin 3t - 3\cos t) + 1$$

$$\begin{aligned} \mathcal{L}^{-1}\left(\frac{10}{s((s+1)^2+9)}\right) &= \frac{10}{3} \int_0^t u(\tau-4) e^{-\tau+4} \sin(3\tau-12) \, d\tau \\ &= \frac{10}{3} u(t-4) \int_4^t e^{-\tau+4} \sin(3\tau-12) \, d\tau \\ &= \frac{10}{3} u(t-4) \int_0^{t-4} e^{-x} \sin 3x \, dx \\ &= \dots \end{aligned}$$

$$\mathcal{L}^{-1}\left(\frac{10e^{-5s}}{(s+1)^2+9}\right) = \frac{10}{3} e^{-t+5} u(t-5) \sin(3t-15)$$

$$\mathcal{L}^{-1}\left(\frac{s+1}{(s+1)^2+9}\right) = \dots$$

$$\mathcal{L}^{-1}\left(\frac{2}{(s+1)^2+9}\right) = \dots$$