Preface

This book is an introductory text intended for graduate students interested in computational mathematics. Some chapters are also suitable for advanced undergraduate students, as well as researchers and practitioners working in related areas. The book introduces numerical methods and selected applications of the Laplacian operator and the Poisson equation. Part I focuses on rectangular meshes and grids, drawing on the second author's lecture notes and projects on numerical PDEs. Part II covers triangulated surfaces and point clouds, derived from the first author's topic courses and projects.

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